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# Hallmark of strong electronic correlations in LaNiO<sub>3</sub>: Photoemission kink and broadening of fully occupied bands

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Recent angular-resolved photoemission experiments on LaNiO<sub>3</sub> reported a renormalization of the Fermi velocity of  $e_g$  quasiparticles, a kink in their dispersion at -0.2 eV and a large broadening and weakened dispersion of the occupied  $t_{2g}$  states. We show here that all these features result from electronic correlations and are quantitatively reproduced by calculations combining density-functional theory and dynamical mean-field theory. The importance and general relevance of correlation effects in filled bands coupled by interorbital interactions to a partially filled band are pointed out.

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## I. INTRODUCTION

The effect of strong correlations in partially filled narrow bands is a central topic in condensed matter physics. Experimental and theoretical studies have revealed their key role in metal-insulator transitions, high- $T_c$  superconductivity, and heavy-fermion behavior. The remarkable development of sophisticated experimental techniques offers novel insights, validates established concepts but also raises new questions. Recently, Eguchi *et al.*<sup>1</sup> performed a delicate soft x-ray angular-resolved photoemission (ARPES) study of LaNiO<sub>3</sub>, a three-dimensional correlated oxide. They found clear signatures of strong correlations in the partially filled quasiparticle band but also, surprisingly, in completely filled bands.

Among the remarkable family of charge-transfer insulators  $RNiO_3$  (with R a rare-earth element),  $^{2,3}$  LaNiO $_3$  is the only one that remains metallic down to the lowest temperatures. Renewed interest in the nickelates has been triggered by the investigation of oxide heterostructures,  $^{4-7}$  and by LaNiO $_3$  being a possible electron analogue of cuprate superconductors.  $^{8-11}$  The nominal electronic configuration of the nickel orbitals is  $t_{2g}^6 e_g^1$ . First-principles calculations based on density functional theory (DFT) show that the  $t_{2g}$  bands are fully occupied and that the two nearly degenerate  $e_g$  bands cross the Fermi level, resulting in a two-sheet Fermi surface.  $^{12,13}$  Clear experimental evidence for strong electronic correlations, such as enhanced effective mass and reduced Drude weight, are revealed by the measurement of the low-temperature specific heat, magnetic susceptibility, resistivity, and thermopower  $^{14-17}$  as well as optical spectroscopy.  $^{18-20}$ 

The ARPES experiment of Eguchi  $et\,al.$  provides important additional insight by revealing several interesting features. First, there is a renormalization of the  $e_g$  quasiparticles Fermi velocity (by a factor of  $\sim 1/3$  as compared to the DFT band structure) at the Fermi-surface crossing near the  $\Gamma$  point. Second, the dispersion of these quasiparticles near  $\Gamma$  displays a "kink" at a binding energy of order -0.2 eV. Finally, in the energy range where DFT predicts dispersive  $t_{2g}$  bands, the ARPES spectra display instead a broad signal that disperses weakly and is shifted towards larger binding energy.

While the Fermi velocity renormalization is consistent with the enhancements observed in thermodynamics and transport measurements, these findings raise the following questions. (i) What is the physical origin of this renormalization and, especially, of the kink structure? (ii) Is the ARPES signal in the [-1.0, -0.5] eV range indeed associated with the  $t_{2g}$  bands, and if so, why is it broad and weakly dispersing?

In this article, we address these questions using a combination of density functional theory and dynamical mean-field theory (DFT + DMFT) as well as model studies. Our results yield a Fermi velocity renormalization and a kink structure in excellent agreement with ARPES, which establishes that both features are a consequence of electronic correlations. We also find that the fully filled  $t_{2g}$  bands have a weakened dispersion and undergo significant broadening. This challenges the naive picture according to which interactions only have a small effect on fully occupied bands. By investigating a simplified model, we explain this finding by the coupling of holes in the fully occupied band to particle-hole excitations in the partially occupied one, due to interorbital interactions. This observation is relevant to other correlated materials in which the energy separation between partially filled and fully occupied bands is small.

## II. MODEL AND METHOD

Our calculations use the full potential implementation of DFT + DMFT detailed in Ref. 21. Well localized Wannier functions<sup>22</sup> are constructed from a large energy window [-7.8,+3.2] eV, which includes all nickel d states and oxygen p states, as appropriate for such a charge-transfer compound with significant hybridization between those states. For simplicity, most calculations were performed for the cubic structure, ignoring the small rhomboedral distortion of LaNiO<sub>3</sub>. Local interactions between Ni-3d states are included in the form  $1/2 U_{mm'}^{\sigma\sigma'} \hat{n}_{m\sigma} \hat{n}_{m'\sigma'}$ . We checked that for the problem at hand the omitted spin-flip and pair-hopping terms are not important. The reduced interaction matrices  $U_{mm'}^{\sigma\sigma}$  and  $U_{mm'}^{\sigma\bar{\sigma}}$  for equal and opposite spins, respectively, are constructed from three Slater integrals  $F^0$ ,  $F^2$ ,  $F^4$  in the usual manner. We

use the standard approximation  $F^4/F^2 \simeq 0.625$  and define the interaction parameters U and J through  $U = F^0$ , J = $(F^2 + F^4)/14$ . Standard values for nickel compounds 19,23 U = 8.0 eV and J = 1.0 eV are used. The double-counting correction term is taken in the "around mean-field" form as customary for metallic compounds  $\Sigma_{dc}^{\sigma} = UN - [U + (M - I)]$ 1)J] $N_{\sigma}/M$ , where M is the number of correlated orbitals, N is the total occupancy and  $N_{\sigma}$  is total occupancy of spin  $\sigma$ . The calculations are fully charge self-consistent, which turns out to be essential in order to insure that the oxygen states are positioned correctly in agreement with PES spectra.<sup>24</sup> We solve the DMFT quantum impurity (embedded atom) problem using the TRIQS<sup>25</sup> toolbox and its implementation of the hybridization expansion continuous-time quantum Monte-Carlo algorithm, <sup>26,27</sup> using Legendre polynomials. <sup>28</sup> The imaginarytime data are continued analytically using the stochastic maximum entropy method<sup>29</sup> and Padé approximants.<sup>30</sup> All calculations were done at a temperature  $T = 1/50 \,\mathrm{eV} \simeq 230 \,\mathrm{K}$ .

## III. PHOTOEMISSION KINK IN $e_g$ BANDS

Focusing first on the  $e_g$  bands, we display on Fig. 1 the spectral intensity in the vicinity of the  $\Gamma$  point. For clarity, the  $t_{2g}$  bands have been projected out. The quasiparticle dispersion obtained by setting the imaginary part of the self-energy to  $0^+$  is also shown as a guide to the eye (dotted line). The Fermi velocity is renormalized, corresponding to an effective mass  $m^*/m \simeq 1/Z \simeq 3$ , in good agreement with experiments. As one moves further away from the Fermi surface crossing, a kink in the dispersion is found, at an energy close to  $-0.2\,\mathrm{eV}$ , followed by a "waterfall" structure corresponding to a rapid broadening of the spectral function. These results agree well with the x-ray ARPES experiments, providing strong evidence for a purely electronic origin of these structures. Indeed, kinks originating from strong electron correlations have been documented in previous DMFT studies at the model

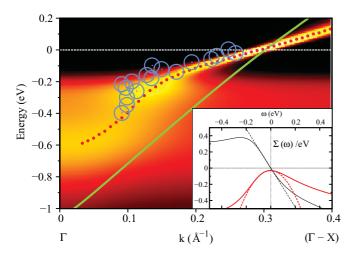


FIG. 1. (Color online) Spectral density map close along  $\Gamma$ -X (close-up), projected onto  $e_g$  character. Dotted line (red): quasiparticle dispersion setting Im $\Sigma=0^+$ . Plain line (green): DFT-GGA band. Open circles (blue): ARPES data. Inset: real (black, thin line) and imaginary parts (red, thick line) of the  $e_g$ -orbital self-energies. Dashed lines: linear (parabolic) fit of the real (imaginary) part.

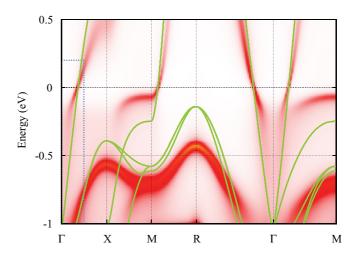


FIG. 2. (Color online) Spectral intensity map (all orbitals). DFT-GGA bands are shown for comparison (green, plain lines). The broadening, shifting, and weaker dispersion of the  $t_{2g}$  states described in the text are clearly apparent. The boundaries of Fig. 1 are also shown (blue, dotted).

level and for other materials.  $^{31-33}$  The kink can be directly related to the  $e_g$  self-energies displayed in the inset of Fig. 1. We note that the low-frequency Fermi-liquid behavior applies only to a narrow frequency range around  $\omega=0$ . A clear deviation, from linearity for Re $\Sigma$  and from quadratic behavior for Im $\Sigma$ , is observed at a negative frequency  $\omega \sim -0.2$  eV. Below this energy scale, Re $\Sigma$  has a kink and bends downwards, while Im $\Sigma$  becomes large so that a quasiparticle description no longer applies.

## IV. BROADENING EFFECTS IN FULLY OCCUPIED $t_{2g}$ BANDS

Now we turn to the  $t_{2g}$  bands. A full map of the spectral intensity including all orbitals is displayed on Fig. 2, for binding energies between -1 and +0.5 eV. It is seen that, in comparison to the DFT-GGA band structure (solid lines), the  $t_{2g}$  states (i) are pushed further below the Fermi level (with, e.g., the top of the band at  $\sim$ -0.4 eV at the  $\Gamma$  point in contrast to  $\sim$  -0.2 eV in DFT-GGA ) (ii) have a weaker dispersion than the band structure result and (iii) importantly, undergo a considerable broadening, due to a rather large scattering rate  $\text{Im}\Sigma_{t_{2a}}(\omega)$  in the energy range from  $\omega \sim -1$  to  $\sim -0.5$  eV, even though the  $t_{2g}$  states are fully occupied. All three facts agree with the ARPES experiments, which report broad and weakly dispersive spectral weight along the  $\Gamma$ -X and M-R directions, and no evidence for dispersive  $t_{2g}$  bands along M-R in the energy range [-0.5, -0.2] eV where DFT-GGA would place these bands. A refined quantitative positioning of the  $t_{2g}$ states would require to take the rhomboedral distortion of LaNiO<sub>3</sub> into account.

Hence, it is seen that the effects of interactions on oneparticle spectra are strong for the  $t_{2g}$  bands, in spite of those bands being completely filled. This may seem surprising if one follows naive intuition drawn from single-band models. However, in a multiband context this is quite natural: a hole created in the occupied  $t_{2g}$  band (as in a photoemission process) can scatter against particle-hole excitations associated with

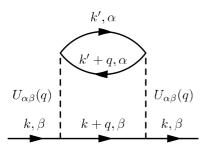


FIG. 3. Second-order contribution to the self-energy.

the partially occupied  $e_g$  states, due to the *interorbital* matrix elements. Consider for example the second-order diagram for the  $t_{2g}$  self-energy shown in Fig. 3 in which a hole in an occupied band  $\beta$  couples through  $U_{\alpha\beta}(q)$  to a particle-hole excitation of band  $\alpha$  described by the corresponding polarization bubble. The latter is proportional to  $n_{\alpha,k'+q}-n_{\alpha,k'}$  and would vanish for a fully filled or empty band, but gives a nonzero contribution if  $\alpha$  is partially occupied. This conclusion persists for higher-order diagrams. This effect has similarities with the physics of x-ray edge singularities and core-hole photoemission, with the important difference that the hole is not static in the present case.

In order to understand this important effect in a simpler setting, we consider a two-band Hubbard model  $H = \sum_{k,m\sigma} \epsilon_k c^\dagger_{km\sigma} c_{km\sigma} - \Delta \sum_i \hat{n}_{i,2\sigma} + U \sum_i \sum_{i,m\sigma < m'\sigma'} \hat{n}_{i,m\sigma} \hat{n}_{i,m'\sigma'}$ . In this expression, m=1,2 is a band index and  $\Delta$  a crystal-field splitting such that the second band is lower in energy. We take both bands to have a semicircular density of states with the same half bandwidth D, U/D=2.0 and no interband hybridization. We set the chemical potential so that there are three electrons per site. This model captures the

transition from a two-band metal into a single-band metal as the crystal-field splitting is progressively increased.<sup>34</sup>

On Figs. 4(a) and 4(b), we display  $\text{Im} \Sigma_m(i\omega_n)$  for imaginary (Matsubara) frequencies, for the lower and upper bands, respectively. The strength of correlations is characterized by the overall magnitude of  $\Sigma_m(i\omega_n)$ . As  $\Delta$  increases, the occupancy of the upper band progressively diminishes from  $n_1 = 1.5$  ( $\Delta = 0$ ) to  $n_1 = 1$  and the strength of correlations in the upper band increases, reflected also in  $Z^{-1} = 1 - \partial \Sigma(i\omega)/\partial(i\omega)|_{\omega\to 0}$  corresponding to the enhancement of effective mass. As soon as the lower band is completely filled  $(n_2 = 2)$ , which happens here at  $\Delta = 0.5D$ ,  $\Sigma_1(i\omega_n)$  saturates and becomes identical to the self-energy obtained in the single-band case  $\Delta \to \infty$  [see Fig. 4(b)]. This is in agreement with the qualitative arguments presented above: no particle-hole excitations can be created (at low energy) in the fully occupied band.

Correspondingly, the correlations in the lower band progressively diminish, as the band is filled-in [see Fig. 4(a)]. However, in contrast to the upper band, no qualitative change is seen at  $\Delta = 0.5D$  and the correlations evolve smoothly as  $\Delta$  is further increased, remaining sizable even at  $\Delta = 1.0D$ . On Figs. 4(c) and 4(d), we display  $\text{Im}\Sigma_2(\omega+i0^+)$  and  $\text{Re}\Sigma_2(\omega+i0^+)$  analytically continued on the real-frequency axis. At  $\Delta = 0$ , the self-energy has a pronounced peak at negative frequencies, corresponding to the pronounced lower Hubbard band. This structure persists through the regime  $\Delta \gtrsim 0.5$  when the lower band is totally filled. To complete the picture, we display on Fig. 5 the energy-resolved spectral functions of the lower band. At the transition point  $\Delta = 0.5D$ , the top of the lower band touches the Fermi level and develops there a sharp quasiparticle peak at  $\omega = 0$ . Most of the spectral weight is carried, however, by a broad structure seen at

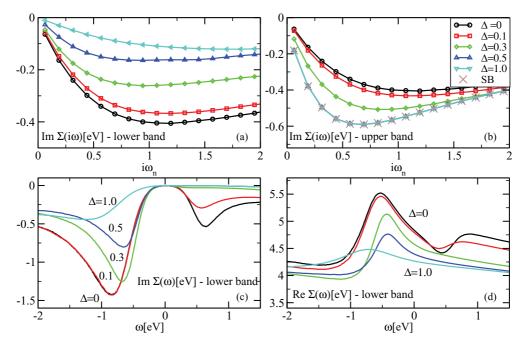


FIG. 4. (Color online) Self-energies of the two-band model with increasing crystal-field splitting  $\Delta$ . Matsubara-frequency self-energy Im $\Sigma_m(i\omega_n)$  of (a) the lower band (fully filled for  $\Delta \geqslant 0.5D$ ) and (b) the higher band (half-filled for  $\Delta \geqslant 0.5D$ ). Single-band (SB) results are shown with crosses. Imaginary (c) and real (d) parts of the real-frequency self-energy for the lower band (analytic continuation using stochastic maximum entropy).

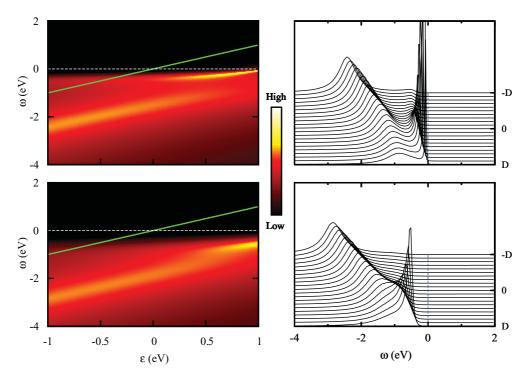


FIG. 5. (Color online) Energy-resolved spectral function for the two-band model  $A_2(\epsilon,\omega) = -\text{Im}[\omega + \mu - \epsilon - \Delta - \Sigma_2(\omega + i0^+)]^{-1}/\pi$ . Left: contour map in the  $(\epsilon,\omega)$  plane with  $-D \leqslant \epsilon \leqslant +D$ . Right: energy  $(\omega)$ -resolved spectra for different energies  $\epsilon + \Delta$  in the band. Upper panel:  $\Delta = 0.5D$ . Lower panel:  $\Delta = 1.0D$ .

negative frequencies. When the lower band lies below the Fermi level ( $\Delta=1.0D$ ), the quasiparticle structure merges with the broad Hubbard like and the energy-resolved spectra are broad for most values of the momentum (except at the very top of the band). Notice that the broadening arises from the coupling to the particle-hole excitations and thus becomes weaker on the Mott insulating side (results not shown), which is opposite to what is found in the previously documented case of hybridization-induced broadening of (e.g., oxygen) bands with mixed-orbital character. Hence the model results fully confirm the qualitative expectations above and clearly demonstrate strong correlation effects in the fully occupied band due to inter-orbital interactions.

#### V. CONCLUSIONS

In conclusion, we have shown that electronic correlations explain the spectral features seen in photoemission experiments on LaNiO<sub>3</sub>. Our DFT + DMFT results are in quantitative agreement with these measurements. While a description in terms of renormalized quasiparticles applies at low energy, <sup>36</sup> the "kink" in the quasiparticle dispersion, shown

here to be of electronic origin, signals the breakdown of this picture. We have demonstrated that interorbital interactions are responsible for the observed large broadening of the fully occupied  $t_{2g}$  states. These correlation effects become important when the occupied band is close to the Fermi energy and hence are relevant to other materials, for example, to the broadening of  $e_g'$  states in Na<sub>x</sub>CoO<sub>2</sub>.<sup>37–39</sup> On a broader level, our results question the applicability of band theory to occupied bands strongly coupled to partially filled ones.

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