# ANONYMOUS BUT AUTHORIZED TRANSACTIONS SUPPORTING SELECTIVE TRACEABILITY

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Abstract: While privacy was more or less neglected in the early days of the Internet, in recent years it has emerged to

be a hot topic in computer security research. Among other reasons, since the use of the Internet is becoming more and more ubiquitous, cloud computing emerges and consequently users provide a lot of information to potentially untrusted third parties. In this paper we propose an approach which provides a means for users to anonymously conduct transactions with a service-provider such that those transactions can neither be linked to a specific user nor linked together. At the same time, a service-provider can be sure that only authorized users are able to conduct transactions. In particular, we bring together the concepts of anonymous authentication from public-key encryption and anonymous as well as unlinkable token based transactions in order to profit from the advantages of the two single approaches. Since full anonymity is usually not desirable, we provide mechanism to identify misbehaving anonymous users behind transactions. More precisely, we realize *selective traceability*, which allows revocation of the anonymity of a suspicious users along with the identification of

all of her transactions, without violating the privacy of all remaining users.

# 1 INTRODUCTION

Today, many services and applications are provided via the Internet resulting in advantageous "anytime, anywhere" access for users. However, privacy becomes a major concern, and its protection is challenging in several ways. Ideally, a user is able to conduct transactions with a service-provider in a way such that a transaction cannot be assigned to an identity (anonymity), nor may two or more transactions be related to each other efficiently (unlinkability). On the other hand, preserving security for the provider requires that only authorized users are able to consume a service and users can be revoked in case of suspicion (traceability).

Interesting applications are in the field of cloudcomputing and especially if even seemingly harmless information about the service-usage behavior, e.g. access frequencies, frequencies of transactions, accessed content, can be valuable information for the service or the cloud provider and needs to be protected from those insiders and wiretappers. One illustrative example is within the healthcare domain, where applications allowing the management of very sensitive health-information for everyone via the Internet, so called Personal Health Records, are growing rapidly (e.g. Google Health, Microsoft Health Vault). In this context, such information can reveal a lot about the state of health of a specific person, e.g. access frequencies will correlate with the state of health. Hence, if such information are available for instance to human resource managers, this could massively influence the chances of getting a job.

# 1.1 Contribution

In this paper we propose an approach to realize anonymous and unlinkable, but authorized service usage based on a combination of anonymous authentication from public-key encryption and one-show tokens obtained from blind signatures. Our approach is especially applicable for services with many users, which dynamically join and leave a service, and frequently conduct transactions with a service-provider. Furthermore, our proposed construction achieves all aspects discussed in the introduction at very low computational overhead, whilst coming at negligible cost for implementation, as only standard (and already widely implemented) public-key cryptography and state of the art smart-cards are used. This is especially of interest, since public-key infrastructures are widely available today.

Our contributions in this paper are manifold. Firstly, we introduce a novel paradigm called postactive anonymous authentication from public-key encryption, which allows us to realize anonymous authentication at the cost of a single decryption for users, in contrast to O(n) decryption resp. encryption operations for schemes known so far. Thereby nis the number of users, the so called anonymity-set. Secondly, we introduce a combination of anonymous authentication from public-key encryption and anonymous one-show tokens from blind signatures. Finally, we present several extensions to one-show tokens including fine-grained validity periods and most notable selective traceability. The latter property means, that a trusted traceability authority is able to link all transactions of a suspicious anonymous user as well as identify this user, without violating the privacy of the remaining users.

### 1.2 Intuition Behind Our Construction

In a nutshell, our construction is as follows. A user registers with a service-provider by providing a public-key of a public-key encryption scheme and registers with a traceability authority. Additionally, we assume that user's are in possession of a tamper resistant smart-card. The service-provider maintains a directory  $\mathcal{D}$  of these public-keys along with a validity of service usage. Users anonymously authenticate against a subset of users in this directory and if the authentication succeeds they obtain a blind signature for a token. On presenting a valid token-signature pair along with a query for a service, the service-provider checks whether the signature is valid, the token was not already used and is valid for the current timeperiod. If all these checks hold, he responds with the answer to the query. Simultaneously, he issues a blind signature for a new token. Consequently, users can conduct sequences of transactions with the serviceprovider. If suspicion occurs, the service-provider can give the token corresponding to a suspicious transaction and the blacklist containing already spent tokens to a traceability authority, who in turn is able to (1) identify the respective user and (2) find all transactions of this user without violating the anonymity of other users (opening tokens of other users). Note, that all actions of users are anonymous and unlinkable.

## 2 RELATED WORK

Several token-based approaches have been proposed so far, although having in mind quite diverge applications. The most prominent are anonymous credential systems introduced in (Chaum, 1985). The basic idea is that users are able to obtain credentials (tokens) for different pseudonyms from different organizations and can prove the possession of these credentials without revealing anything more than the fact that they own such credentials. Over the years there have been proposed different approaches to design anonymous credential systems providing quite different functionalities (Lysyanskaya et al., 2000; Camenisch and Lysyanskaya, 2001; Verheul, 2001). Although anonymous credential systems are very powerful, realizing identity-escrow, limiting the number of showings as well as realizing dynamical joining and revoking of users comes at high computational costs. Furthermore, we do not focus on systems that involve multiple credential (token) issuers and verifiers and are looking for more efficient solutions.

Another class of schemes are multi-coupon (MC) systems (Canard et al., 2006; Chen et al., 2007), whereas a MC represents a collection of coupons (or tokens) that is regarded as a single unit. Basically, a user is issued a batch of tokens (which are tied together) and is allowed to spend one token after another in an anonymous and unlinkable fashion. The most sophisticated schemes (Canard et al., 2006; Chen et al., 2007) are based on signature schemes that allow users to obtain signatures on (committed) sequences of messages and provide efficient zero-knowledge proofs of knowledge of signatures and properties of signed message elements (Camenisch and Lysyanskaya, 2002; Camenisch and Lysyanskaya, 2004). Although these schemes are conceptually very elegant, they are quite expensive and do not provide (selective) traceability.

Recently, a scheme for anonymous subscriptions, based on one of those signature schemes was proposed in (Blanton, 2008). The concept is very appealing and it provides an elegant solution to realize validity-periods of subscriptions using zero-knowledge range proofs, but it does not support (selective) traceability, which is an important feature of our construction. Another construction of (Camenisch et al., 2006) focuses on *n*-times anonymous authentication, which allows to identify a user if he

$\begin{array}{c} \textbf{User} \\ SK_{u_i} \end{array}$		Verifier ${\cal D}$
		$c \in_R \{0,1\}^{\kappa}$
c	<b>←</b>	$\mathbf{c} = (E_{PK_{u_1}}(c), \dots, E_{PK_{u_n}}(c))$
$c' = D_{SK_{u_i}}(\mathbf{c}[i])$		$c' \stackrel{?}{=} c$

Protocol 1: Anonymous authentication from PKE.

spends more than n tokens within one time-period. However, they also do not focus on selective traceability.

To the best of our knowledge, the only solution to selective traceability so far are traceable signatures (Kiayias et al., 2004; Libert and Yung, 2009), which are, however, rather of theoretical interest. In conclusion, none of the aforementioned approaches provides an efficient way to realize selective traceability, whereas our construction presented in this paper achieves this goal at a reasonable overall cost.

# 3 POSTACTIVE ANONYMOUS AUTHENTICATION

In this section we present a novel paradigm for anonymous authentication schemes from public-key encryption (PKE), which we call *postactive anonymous authentication*. Anonymous authentication from public-key encryption and its application is not absolutely new (Schechter et al., 1999; Lindell, 2007; Xi et al., 2008; Slamanig et al., 2009), but allows a convenient way for a prover to anonymously authenticate to a verifier providing user-chosen bandwidthanonymity trade off. More precisely, users can determine on their own the size of the anonymity-set (as a subset of all users) and consequently determine the bandwidth consumption of the protocol (see below).

# 3.1 Deterministic from Probabilistic Public-Key Encryption

The notion of deterministic public-key encryption was introduced in (Bellare et al., 2007). Basically, the idea behind this concept is to turn any probabilistic PKE into a deterministic scheme. One general and efficient construction is the so called "Encryptwith-Hash" (EwH) construction introduced in (Bellare et al., 2007), which will be discussed subsequently. An EwH scheme is based on a probabilistic

PKE scheme and deterministically encrypts a plaintext m by applying the encryption algorithm of the probabilistic scheme, whereas the used random coins  $\omega$  are not chosen uniformly at random, but are computed as a hash of the public key PK and the plaintext m. Consequently, everybody who knows a message m and a ciphertext c (presumably an encryption of m), can deterministically infer the random coins used for the encryption, i.e. compute  $\omega = H(PK, m)$  and  $c^* = E_{PK}(m; \omega)$  and check whether the encryption  $c^*$  computed by him equals the given ciphertext. If  $c^* = c$  holds, they are both encryptions of the same message m. It should be noted that the output of the hash-function needs to be suitable for the use as random coins in the respective PKE scheme.

# 3.2 Anonymous Authentication from Public-Key Encryption

Loosely spoken, the basic idea behind anonymous authentication protocols is that a verifier runs n parallel instances of a challenge-response protocol based on public-key encryption using *n* distinct public keys with one anonymous prover, who represents n "virtual" provers (we call this set the anonymity-set). Recall, in a challenge-response protocol authentication is achieved by demonstrating the ability to correctly decrypt an encrypted challenge. In anonymous authentication, the verifier chooses one (fixed) challenge and encrypts it with everyones public-key (of the anonymity-set). Hence, if the prover is able to provide the challenge bit-string to the verifier, the verifier can be sure that the unknown prover is in possession of at least one secret which corresponds to one of the n public-keys. In protocol 1, we assume that a user  $u_i$  authenticates against a directory  $\mathcal{D} = ((ID_{u_1}, PK_{u_1}), \dots, (ID_{u_n}, PK_{u_n})).$ 

However, the verifier can cheat by encrypting distinct challenges  $c_1, \ldots, c_n$  for distinguishing different responders based on the specific challenge. If the encryptions of all ciphertexts in the challenge-sequence are deterministic (such as RSA or Rabin's

scheme), then  $u_i$  may as well encrypt  $c_i$  using all remaining public-keys to see whether or not the challenges match (Schechter et al., 1999). This is what we call trial encryptions. The same can be done by turning probabilistic public-key encryption schemes into deterministic ones (see section 3.1) as proposed in (Slamanig et al., 2009), which is no longer prone to known security flaws of the aforementioned schemes and retains the efficiency. Nevertheless, the computational effort for the user is linear in the size of the anonymity-set in any case and furthermore the user needs to be in possession of all other public-keys. To reduce the computational effort, users could perform trial encryptions only for a reasonably small randomly subsequence of the challenge-sequence resulting in more efficient protocols providing probabilistic anonymity (Slamanig et al., 2009). However, the need for the public-keys of the respective users still remains.

## 3.3 Postactive Anonymity

The basic idea behind postactive anonymous authentication is that users do not compute trial encryptions anymore, but post their received challenge-sequence along with the signature for the challenge-sequence of the verifier along with the decrypted random challenge to a public bulletin-board. Clearly, this should not be done until the user has successfully authenticated and the challenge is invalidated.

Now, we assume that users help each other and visit the bulletin-board frequently to check whether the verifier behaves honest. This can be done, when deterministic PKE schemes (obtained by applying the EwH construction discussed in section 3.1) are used and the challenge (the plaintext) is known. If a user notices that a verifier has cheated, the user can show this transcript to a judge and can convince him that the verifier has cheated. Since the verifier has digitally signed the transcript, he cannot repudiate the cheating behavior. The verifier can still cheat in this scenario and thus identify a single user who authenticates anonymously, but his trustworthiness is in jeopardy as he is likely to be caught.

The beauty of post-active anonymity is that it passes back the full risk to the dishonest verifier: if he attempts to discover an anonymous enquirer, then he takes a high risk of loosing the trust of the community. Postactive anonymity therefore makes honesty verifier's best behavior strategy. Furthermore, it should be noted that this paradigm provides a superior feature, namely users may register public-keys of arbitrary cryptosystems and only the verifier needs to support all algorithms (and those users checking

entire challenge-sequences). The user solely uses the respective algorithm corresponding to his publickey cryptosystem and furthermore needs to compute only one decryption operation. This results in a low and constant computational effort, whereas all other approaches require effort *linear* in the size of  $\mathcal{D}$ , which can be enormous for large sets of authorized users. However, it should be noted that the size of the ciphertext-sequence grows linear with the size of  $\mathcal{D}$ , which can be quite large. In these cases, users may randomly choose a subset  $\mathcal{D}' \subset \mathcal{D}$  for their anonymity-set such that the size of the ciphertextsequence is acceptable. For instance, if the publickey encryption scheme of choice will be ElGamal (ElGamal, 1984) on Elliptic Curves  $E(\mathbb{Z}_p)$ , where p is a prime with |p| = 192 bits, then, a choice of the anonymity-set with  $|\mathcal{D}'| = 100$  will lead to a ciphertext-sequence of  $\approx 5$  KB, which is reasonably small.

## 4 OUR APPROACH

To realize anonymous and unlinkable but authorized transactions, we briefly review the concept of blind signatures and provide a generic construction of a protocol for such transactions based on one-show tokens from blind signatures. Thereafter, we introduce our approach by combining postactive anonymous authentication with such one-show tokens. Subsequently, we gradually augment this construction to achieve (1) fine-grained validity periods for tokens, (2) selective traceability and (3) discuss how to prevent resp. detect cloning attacks.

### 4.1 Blind Signatures

Blind signatures are a well known cryptographic primitive introduced in (Chaum, 1982), which provide a means such that an entity is able to obtain a valid signature on a message without the signer being able to learn anything about the message at the time of signing. More precisely, the signer actually signs a randomly blinded message and the resulting signature can subsequently be unblinded by the originator, wheres the originator obtains a valid signature for the original message. Consequently, the signed message cannot be linked to the originator by the signer. We rely our construction on efficient twomove blind signature schemes. Therefore, we can take the RSA based scheme of (Chaum, 1982), which was proven to be secure for the full-domain hash RSA scheme (FDH-RSA) in the random oracle model under the chosen-target-one-more-RSA-inversion as-

$\mathbf{User} \\ \mathbf{t_i} = (t_i, \sigma_{t_i}), PK$	Service-Provider SK,BL
$\frac{\texttt{create}t_{i+1}}{t_{i+1}} = B(H(t_{i+1}))$	
$(\mathbf{t}_i, \overline{t_{i+1}}, Q_i)$	 $(\mathbf{t}_i,\overline{t_{i+1}},Q_i)$
	$t_{i} \notin BL$ $V_{PK_{V}}(H(t_{i}), \sigma_{t_{i}}) \stackrel{?}{=} accept$ $\sigma_{\overline{t_{i+1}}} = S_{SK_{V}}(\overline{t_{i+1}})$
$(\sigma_{\overline{t_{i+1}}},R_i)$	 $(\sigma_{\overline{t_{i+1}}},R_i)$
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Protocol 2: Simple Blind Signature-Based Transactions (SBSBT).

sumption (Bellare et al., 2003). Alternatively, we can take the blind signature scheme form (Boldyreva, 2003) which is based on the BLS signature (Boneh et al., 2004) and is provably secure in the random oracle model under the chosen-target Computational-Diffie-Hellman assumption. Subsequently, we abstract from the concrete protocol and denote the blinding operation of a message m as  $\overline{m} = B(m)$  and the unblinding of the signature  $\overline{\sigma}$  as  $\sigma = B^{-1}(\overline{\sigma})$ .

# 4.2 Anonymous Unlinkable One-Show Tokens

Below, we provide a generic protocol to obtain oneshow tokens from a verifier which can be shown to the same party (spent) in an anonymous and unlinkable fashion. The basic idea behind this construction was proposed in (Stubblebine et al., 1999), however, providing non of the functionalities discussed in this section and not combined with anonymous authentication.

We define a token as a simple data-structure which can be described as a tuple  $(id_t, id_{sp}, id_s)$ , whereas  $id_t$  is a unique token-ID,  $id_{sp}$  is an ID of the service-provider and  $id_s$  may represent an ID of the respective service (the token may be augmented by further elements, e.g. validity-period, as discussed subsequently in this section). We want to note, that what we denote as a token is often also referred to as a ticket, a credential, a coupon, a transaction-pseudonym or a one-time-pseudonym.

For now, assume that user  $u_i$  holds an initial tokensignature pair  $\mathbf{t_i} = (t_i, \sigma_{t_i})$  from the service-provider (also denoted as the verifier V, for short), e.g. the user registers to the service-provider, pays and obtains a signed token  $\mathbf{t}_i$ . Furthermore, assume that the service-provider generates a key-pair with suitable

parameters for issuing blind signatures, with publickey  $PK_V$  and private-key  $SK_V$ . The generic protocol for conducting anonymous and unlinkable transactions with V is illustrated in protocol 2. In order to make the tokens one-time-usage-only, the verifier maintains a blacklist BL to blacklist already seen tokens and discard tokens upon seeing them again. Assume now that user  $u_i$  wants to authorize a query  $Q_i$  to the service-provider. In order to obtain a new signed token for another transaction,  $u_i$  computes a blinded token  $\overline{t_{i+1}} = B(H(t_{i+1}))$ , whereas H denotes a suitable collision resistant cryptographic hash function and  $t_{i+1}$  represents a new token. User  $u_i$  sends  $(\mathbf{t}_i, \overline{t_{i+1}}, Q_i)$  to the verifier, who checks whether the token is well formed and the ID of  $t_i$  is not already contained in the blacklist. If this holds, he computes  $\sigma_{\overline{t_{i+1}}} = S_{SK_V}(\overline{t_{i+1}})$ , i.e signs the blinded token, and sends the resulting signature  $\sigma_{\overline{t_{i+1}}}$  along with the result  $R_i$  of the query  $Q_i$  back to  $u_i$ . The user in turn unblinds the signature and obtains  $\sigma_{t_{i+1}} = B^{-1}(\sigma_{\overline{i+1}})$ , a valid signature for  $H(t_{i+1})$ . Consequently,  $u_i$  can use  $\mathbf{t}_{i+1}$  to authorize a new transaction resp. query  $Q_{i+1}$ for some data at the verifier.

# 4.3 A Combined Approach

The idea is to combine the aforementioned approach to realize one-show tokens with the concept of anonymous authentication. It should be noted that one could use several classes of anonymous authentication schemes for this purpose, e.g. ring signatures (Rivest et al., 2001), group signatures (Ateniese et al., 2000), but we will assume that anonymous authentication from public-key encryption (PKE) is used. The combination can be realized as follows:

1. **Registration:** Initially a user  $u_i$  registers once to the service-provider (verifier) by providing iden-

tifying information  $ID_{u_i}$  together with a the user's public-key  $PK_{u_i}$ . The verifier adds the user and the public-key to the public directory  $\mathcal{D}$  of authorized users.

- 2. **Authentication:** The user anonymously authenticates to the verifier and after a successful authentication the user obtains a blind signature for a token  $t_0$  and thus holds a token-signature pair  $\mathbf{t}_0 = (t_0, \sigma_{t_0})$  for a subsequent transaction. Later, the user posts the challenge-sequence along with the signature and the challenge such that other users can check whether the service-provider cheats.
- 3. **Access:** The user provides **t**<sub>0</sub> and a new blinded token together with a query to the verifier and obtains a response, which is either a response to the query and a signature on the new blinded token for a subsequent transaction or an indication that the transaction was not authorized.

The register procedure is carried out once for every user. In order to obtain access to the system, a user conducts the authentication procedure with the verifier. Every authentication procedure is connected to a set of subsequent transactions, whereas the number of sequenced transaction is *not* limited by the verifier. Subsequently, we will discuss how a subscription of a user can be terminated, since this is impossible in the aforementioned setting.

# 4.4 Fine-Grained Validity Periods

A natural and efficient approach to exclude users from being able to conduct further transactions be realized as follows:

- The service-provider discretizes the time into time-periods  $\Delta_0, \Delta_1, \ldots$  of duration  $d_{\Delta_i}$  (they may also differ for different time-periods) and assigns a unique random number  $\delta_i$  to every time-period  $\Delta_i$ . The most important point is, that the service-provider solely publishes  $\delta_i$  for the current time-period  $\delta_i$  and given all random numbers of previous and the actual time-periods it is infeasible to compute  $\delta_j$  for some future time-period.
- The random number  $\delta_i$  needs to be included into the token by the user, otherwise the token will be rejected. Hence, we augment our token by an additional element and tokens can now be represented as a tuple  $t = (id_t, id_{sp}, id_s, \delta_i)$ . Within a time-period an authorized user can obtain an "initial" token by means of a successful anonymous authentication.
- Service-providers can easily manage the termination of service accesses of a user by removing a

- user from the directory  $\mathcal{D}$ . It should be noted, that the termination of service access during a time-period is impossible, but the service-provider is able to control the granularity by choosing adequate durations of time-periods.
- Since the validity of tokens is restricted to a specific time-period, the service-provider solely needs to blacklist tokens within the actual period. Due to the limited duration, the blacklist is bound in size and previous blacklists can be discarded, which makes the approach entirely practical from this point of view.

# 4.5 Selective Traceability

Traceability in this context means, that a trusted third party (TTP), a so called traceability authority (TA), is able to identify the owner of a token as well as it's position within a sequence of transactions conducted by a user. Besides, it is desirable to achieve selective traceability for all tokens of the user within a specific time-period  $\Delta_i$ . This means, that all tokens of a suspicious user can be found, without violating the privacy of other users. But it is important, that the serviceprovider has no means to revoke the anonymity of honest users by himself. In order to achieve this, we require the user to register a pseudonym  $\gamma_{u_i}$  (which is randomly sampled from an appropriate space) with the TA, and this pseudonym is solely known to the TA and the user's smart-card (and not to the serviceprovider). The tamper resistant smart-card of the user has to maintain an internal counter cnt, which is initialized to a fixed user-specific value (which we will discuss below) during every instance of an anonymous authentication protocol and incremented during every generation of a new token.

Basically, the user's smart-card includes additional traceability information e into the token on behalf of the user. Hence, every token t will be augmented by an element e and will be a tuple  $t = (id_t, id_{sp}, id_s, \delta_i, e), \text{ where } e = E_{PK_{TA}}(\gamma_{u_i}, \text{cnt}_{u_i}; \omega)$ represents a probabilistic encryption of the tuple  $(\gamma_{u_i}, \operatorname{cnt}_{u_i})$  under TA's public-key. Note that  $\omega$  are the random coins for the probabilistic encryption algorithm, which will be discussed below. After computing a token, the smart-card increments the counter  $cnt_{u_i}$  for the next token. In order to avoid partial knowledge about the plaintext we choose user- and time-period-specific start values of counters by computing the initial value of  $cnt_{u_i}$  denoted as  $cnt_{init}$ (which is initialized during every anonymous authentication) based on a suitable pseudorandom function. Working in the random oracle model, we can use a suitable cryptographic hash function H and compute the initial value as  $cnt_{init} = H(\gamma_{u_i}, \delta_j)$  which provides us an initial counter value that depends on the pseudonym and on the current time-period.

## 4.5.1 Tracing of Single Showings

It is obvious that in case of suspicion the respective token (which is maintained by the service-provider in his blacklist) can be given to the TA, which in turn can decrypt e and obtain the pseudonym of the user. Consequently, the identity corresponding to the user's pseudonym can be returned to the service-provider. To prevent this user from being able to conduct any future transaction, the service-provider has to remove the respective user from his directory  $\mathcal{D}$  used for authentication. Consequently, this user will no longer be able to conduct anonymous authentications with the system. In this setting, the TA is very powerful, since it can identify all users behind all transactions. However, we assume that the TA is trusted and only provides "necessary" information to the service-provider if and only if the service-provider can credibly argue that fraud or misuse has happened. It should be noted, that in order to decrease the trust, we could share the private-key of the TA among a set of TA's and perform threshold-decryption to reveal the identity of a user.

### 4.5.2 Efficient Selective Traceability

It order to protect the privacy of other (innocent) users and to reduce the amount of workload for the TA, we propose a novel way to achieve selective traceability. Trivially, the TA could realize this feature by decrypting all remaining tokens in the blacklist and picking out those of the suspicious users. However, we want to protect the privacy of the remaining users and go the other way round. Essentially, the TA re-encrypts potential escrow information of the user and searches the blacklist for these potential values. How this is achieved will be discussed in the following. The TA knows the counter value cnt<sub>act</sub> and the pseudonym of the user by decrypting the escrow information e of the suspicious token. Since the TA also knows that the counter is incremented during the creation of a new token and knows the value for the current time-period  $\delta_j$ , it is able to compute the starting value of the user as  $cnt_{init} = H(\gamma_{u_i}, \delta_j)$ . Consequently, the TA has to look for tokens in the counterinterval  $[cnt_{init}, cnt_{act} + k]$ , where k is some positive integer. Basically, the TA looks k tokens ahead from the start, since it cannot determine the actual number of transaction of the suspicious user within his "session". The concrete choice of k mainly depends on the application, however, when assuming that transactions are distributed uniformly among users we could take  $k = \overline{|BL|}/|\mathcal{D}|$ , where  $\overline{|BL|}$  represents the arithmetic mean of the sizes of all previous blacklists.

Now, we need a measure for the TA to actually find the respective tokens within the blacklist. This can be easily achieved by converting the probabilistic public-key encryption scheme used by the TA into a deterministic one, i.e. by applying the EwH construction. We apply exactly this strategy to the construction of the escrow information e. More precisely, we construct the random coins  $\omega$  for the encryption algorithm as  $\omega = H(PK_{TA}, (\gamma_{u_i}, \operatorname{cnt}_{u_i}))$ , whereas  $PK_{TA}$  is TA's public-key. Algorithm 1 illustrates how the TA realizes selective traceability when given a suspicious token and the blacklist of the service-provider.

### Algorithm 1 Selective Tracing

**Input:** A suspicious token  $\tilde{t} = (t, e)$ , the value  $\delta$  of the current time-period, a parameter k, a blacklist BL and a key-pair  $(PK_{TA}, SK_{TA})$  of a public-key encryption algorithm.

**Output:** A sequence  $T = (\tilde{t}_1, \dots, \tilde{t}_n)$  of transactions.

```
(\gamma, \operatorname{cnt}_{act}, \delta) \Leftarrow D_{SK_{TA}}(e)
\operatorname{cnt}_{init} \Leftarrow H(\gamma, \delta)
pos \Leftarrow 0;
for all i = \operatorname{cnt}_{init} to \operatorname{cnt}_{act} + k do
\omega_i \Leftarrow H(PK_{TA}, (\gamma, i))
e_i \Leftarrow E_{PK_{TA}}(\gamma, i; \omega_i)
\tilde{t}_i \Leftarrow \operatorname{searchBL}(e_i, BL)
if \tilde{t}_i \neq \operatorname{null} then
T[pos] \Leftarrow \tilde{t}_i
pos + +
end if
end for
return T
```

The algorithm searchBL simply searches the black-list BL for tokens with escrow information  $e_i$ . By realizing the strategy discussed above, the workload of the TA can be significantly decreased. If we denote the size of the interval  $[\operatorname{cnt}_{init}, \operatorname{cnt}_{act} + k]$  by m, we achieve O(m) encryption operations over O(n) decryption operations in the trivial case, since we can assume that  $m \ll n$  holds. Furthermore, the privacy of innocent users does not need to be violated.

# 4.6 Enforcing Traceability

A very simple attack to circumvent the traceability property is as follows. Assume that the smart-card performs the identity-escrow on behalf of the user and assume further that the user behaves malicious, i.e. wants to hinder the TA to identify him in case of fraud or misuse. Therefore, assume that a user is currently conducting transactions and obtains a response R along with the blind signature  $\sigma_{\bar{t}}$  for the new token from the service-provider in the first step (it could, however, also be the initial transaction). The user passes the signature to his smart-card, which in turn computes  $\sigma_t = B^{-1}(\sigma_{\bar{t}})$ , generates a new blinded token  $\bar{t}'$  (including the traceability information e) and passes the tuple  $(t,\sigma_t,\bar{t}')$  to the user. Although  $\bar{t}'$  is well-formed, the malicious user can easily replace  $\bar{t}'$  with another blinded token  $\bar{t}''$  that is nearly well-formed. More precisely, the token is well-formed, except for the traceability information (which could either be chosen at random or represents the encryption of some random value).

The conceptually most straightforward approach to solve this problem is, that the smart-card simply encrypts the tuple  $(t, \sigma_t, \bar{t}')$  under a service-provider's public-key of a secure public-key encryption scheme. Consequently, the user will never have access to a tuple of the form  $(t, \sigma_t)$ , which would allow him to conduct a transaction with a replaced "self-constructed" non-traceable new blinded token t''. However, the public-key of the service-provider needs to be integrated into the smart-card in an authentic fashion. Otherwise, a malicious user can easily mount a person-in-the-middle attack by providing some arbitrary public-key (for whom the corresponding privatekey is known to the user) to the smart-card. Consequently, the user can decrypt the ciphertext and obtain a tuple  $(t, \sigma_t, \overline{t}')$  which he can modify to  $(t, \sigma_t, \overline{t}'')$  and send this tuple encrypted under the service-provider's public-key.

# 4.7 Cloning Protection

The drawback of fine-grained validity periods is, that it is potentially susceptible to what we call the cloning-attack. Loosely spoken, this attack means that a fraudulent authorized users may obtain valid token-signature pairs that he can make available to a set of unauthorized users. These users, the so called *clones*, are consequently able to anonymously conduct a sequence of transactions with the serviceprovider within the respective time-period, although they are not authorized to do so. Note that this attack is still possible when the smart-card only gives the ciphertext of the tuple  $(t, \sigma_t, \bar{t}')$  to the user. However, the attack is somewhat reduced, since the clone will solely be able to conduct a *single* transaction. By applying counters cnt as discussed in section 4.6, this attack is easy to detect. Therefore, the serviceprovider only has to search for identical escrow values e in his blacklist.

• If a user  $u_i$  gives away his encrypted tuple

 $(t_0, \sigma_0, \overline{t_1})$  to a clone and the clone spends the token, the entry in the blacklist will contain traceability information  $e_0 = E_{PK_{TA}}(\gamma_{u_i}, \operatorname{cnt}_{u_i}; \omega)$ , whereas  $\omega = H(PK_{TA}, (\gamma_{u_i}, \operatorname{cnt}_{u_i}))$  and  $\operatorname{cnt}_{u_i} = H(\gamma_{u_i}, \delta_i)$ .

• If the user authenticates again within the same time-period, the traceability information  $e'_0$  of the token  $t'_0$  will be identical, since the counter is reinitialized to  $\operatorname{cnt}_{u_i} = H(\gamma_{u_i}, \delta_i)$ .

Hence, if the service-provider detects such a cloning attack (tokens where  $e_i = e_j$  for some  $i \neq j$ ), he can give both entries of the blacklist to the TA to revoke the anonymity of the misbehaving user. It should be noted, that this could be problematic in case of broken connections. The service-provider could have different strategies for handling this, whereas we briefly sketch two of them below.

Upon presenting exactly the same token multiple times, the service-provider may re-send the response to the query Q attached to the respective token  $\mathbf{t}$ . However, that incidence should be indicated by *not* attaching a query, whenever re-showing a token, as this query has been submitted anyway. Still, a request to re-send the answer should come with the token, in case the query did not make it through in the first instance. However, if neither is done, and a known token  $\mathbf{t}$  with a new (different to the previous) query Q' ( $\neq Q$ ) is coming in, then the verifier should become wary and start tracing. This ensures robustness of the protocol as well it creates a simple mechanism to detect piracy

Alternatively, the service-provider could realize some kind of glitch-tolerance, by defining some threshold *K* of "clone-activity", which need to be reached before revoking users.

### 5 SECURITY ANALYSIS

In this section we will discuss the threat model and investigate the security of the proposed construction. Therefore, we assume that users communicate their messages to service-providers over a communication channel that provides perfect anonymity and unlinkability of exchanged messages, as it is the case with all interactive protocols providing such features.

### 5.1 Threat Model

We assume that the manufacturer of the smart-cards is trustworthy and hence the smart-cards are tamper resistant and do not contain any backdoors, Trojan horses, etc. Furthermore, users are assumed to be

dishonest (active adversaries), i.e. will actively try to fool the service-provider resp. authorize unauthorized users, which is a reasonable assumption for real-world scenarios. Service-providers are honest-but-curious, i.e. follow the protocol specification but use any gathered information in order to try to identify anonymous users. However, service-providers can also be active adversaries, but only with respect to the anonymous authentication protocol.

# 5.2 Anonymous Authentication

For the used anonymous authentication protocol we require anonymity, correctness, unforgeability and unlinkability, which can be proven to hold for existing protocols (Slamanig et al., 2009; Lindell, 2007). However, the known definitions of anonymity and unlinkability are less formally ensured in the post-active anonymity setting. Clearly, anonymity can be broken if the verifier encrypts distinct random challenges, which consequently can restore linkability too. However, it is equally obvious that a cheating verifier acts completely on his own risk, as the community will accuse him of being dishonest. In that case, the service will not be used any more, and a cheating verifier could loose more than he could win. The correctness and unforgeability properties are retained, since solely trial encryptions are omitted. Finally, it should be noted that when using standard anonymous authentication (Schechter et al., 1999; Slamanig et al., 2009; Lindell, 2007), we obtain security with respect to existing definitions, however, at substantially higher costs.

## 5.3 Security of Our Construction

In our investigation of the security of the construction we investigate the anonymity of transactions, the unlinkability of transactions and the unforgeability of tokens. We inspect every property below and sketch the ideas:

**Transaction anonymity:** Every token showing integrates the issuing of a new token. Hence, we firstly need to look at the token which is shown and secondly the blinded token which is signed by the verifier. The anonymity of the token *t* shown reduces to inspecting the escrow information *e*. The anonymity follows from two observations concerning the escrow information *e*. Firstly, (Bellare et al., 2007) prove that for any at least IND-CPA secure probabilistic public-key encryption that is converted into a deterministic one (by applying the EwH construction), it holds that an adversary provided with encryptions of plaintexts drawn from a message-space

of high min-entropy (which is clearly the case, since we encrypt randomly chosen pseudonyms along with a value obtained by evaluating a pseudorandom function on this value) will have negligible advantage in computing any public-key independent partial information function of the plaintexts (this notion is called PRIV in (Bellare et al., 2007)). Hence, the so obtained deterministic public-key encryption scheme provides the required security guarantees and can be seen as a computationally hiding commitment. Secondly, the pseudonyms of users are sampled at random from a large enough space and are solely known to the TA and the user's smart-cards (which are assumed to be tamper-proof). Consequently, any adversary can solely guess the respective pseudonym of a user, which would allow him to identify or trace one user. By choosing the space for the pseudonyms accordingly large, this probability can be made negligible. The anonymity of the blinded token follows from the properties of the blind signature scheme.

**Unforgeability:** Since the smart-card solely gives ciphertexts of tuples  $(t, \sigma_t, \bar{t}')$  to the users, a user would need to forge a signature from the verifier. However, this means that a user would need to existentially forge a signature for the signature scheme underlying the blind signature scheme.

**Unlinkability:** The unlinkability of the issuing and showing of a token t reduces to the blindness property of the used blind signature scheme. Hence, there is no way for the signer to relate the issuing and showing of a token. Furthermore, we need to look at the unlinkability of different showings, which means that it cannot be decided whether a set tokens was shown by the same user. Therefore, our argumentation is similar to that used for the transaction anonymity property. Let us assume without loss of generality that we have two tokens t and t'. Only e and e' contain information about the user. However, as already discussed in context of transaction anonymity e and e' are computationally hiding commitments.

## **6 FUTURE ASPECTS**

One drawback of the approach presented in this paper is that we cannot realize a fine-grained access control for resources connected to services. However, this can be solved by using partially blind signatures (Abe and Fujisaki, 1996; Abe and Okamoto, 2000) instead of blind signatures. Loosely spoken, in a partially blind signature scheme, a receiver blinds a message m, obtains  $\overline{m} = B(m)$  and sends  $\overline{m}$  to the signer. The signer computes a partially blind signature  $\overline{\sigma} = S_{SKS}(\overline{m}, \text{info})$ , which includes a common information

info and sends  $\overline{\sigma}$  to the receiver. The receiver unblinds  $\overline{\sigma}$  by computing  $\sigma = B^{-1}(\overline{\sigma})$ , can verify whether the common information info was included and obtains a valid signature  $\sigma$  for the tuple (m, info). Note, that the message m is entirely unknown to the signer. We can use them as follows: The service-provider defines the set of privileges P (which are connected to resources of services) and during registration privileges are assigned to users. By choosing the anonymity-set according to required privileges (users which have the same privileges) an encoding of these privileges can be integrated by means of common information info into the blinded token. Hence, when presenting the token, the service-provider can decide whether a query Q will be authorized or not. It should be noted, that anonymity and unlinkability are preserved.

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