

# Impact of Geological Surface Density Information and Seismic 3D Density Models for High Precision Regional Geoid Computation

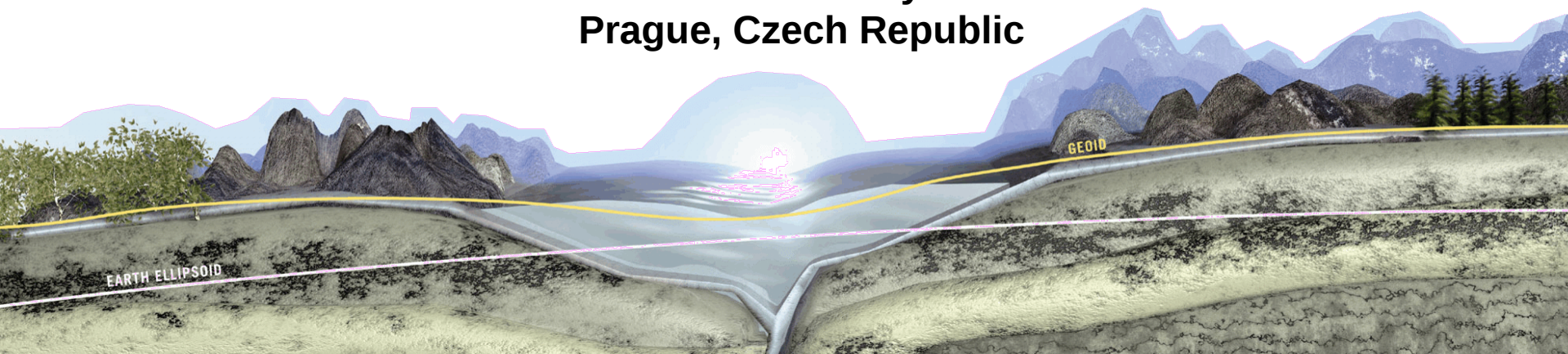
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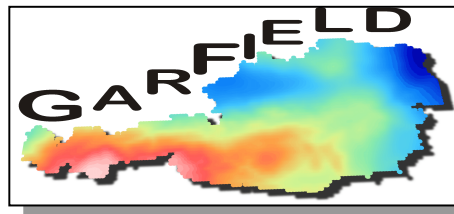
**International Union of Geodesy and Geophysics  
(IUGG)**

**General Assembly 2015  
Prague, Czech Republic**



# Introduction

- Focus of investigations:
  - **Density information**
  - **How does this data type can contribute to an improved geoid?**
  - **Different validation approaches**
- Investigations are embedded in the current Austrian geoid initiative “*Geoid for Austria - Regional gravity FIELD improved*” (GARFIELD) - P25222-N29

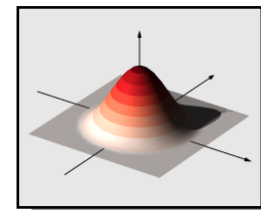
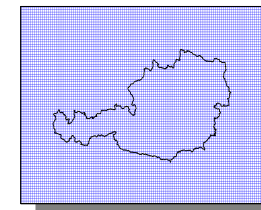
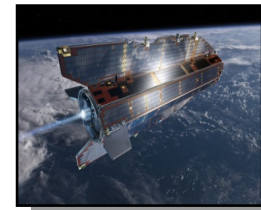


- **Question:**
  - ***Used computation parameters?***

# Computation Parameters

- **Remove-Compute-Restore** technique
- Terrestrial data:
  - **72327** gravity measurements
  - **735** deflections of the vertical
  - **192** GPS/Leveling observations
  - **192** geopotential numbers
- Global gravity field model:
  - **GOCO05s** up to d/o 250
- Topographic reduction: **Prism formula**
  - DTM 176 x 196 m within central Europe
  - **3 density models** interpolated to DTM spacing
- Computation: **Least squares approach**
  - Radial basis function parametrization

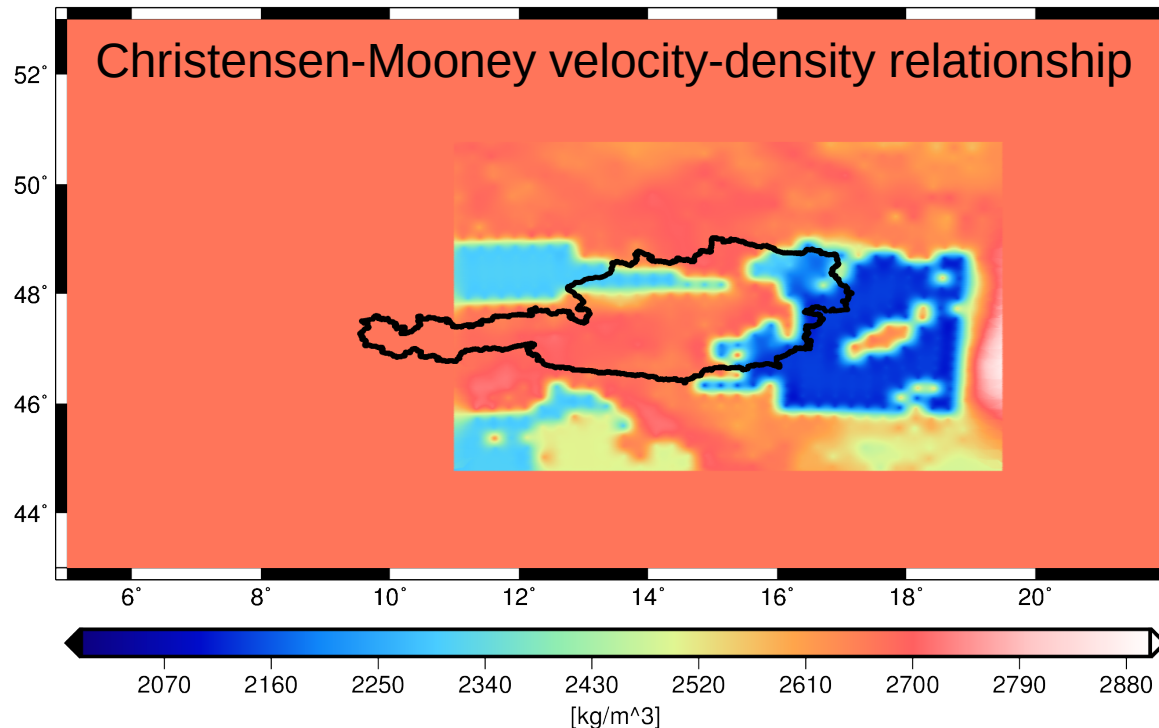
} Used for validation



# Density Models (1)

- **3D seismic data  $\rho_{seis}$ : 11 layers (0 to -10 km), 1 km vertical spacing**
  - Top layer refers to sea level → used as lower boundary in combination with surface density

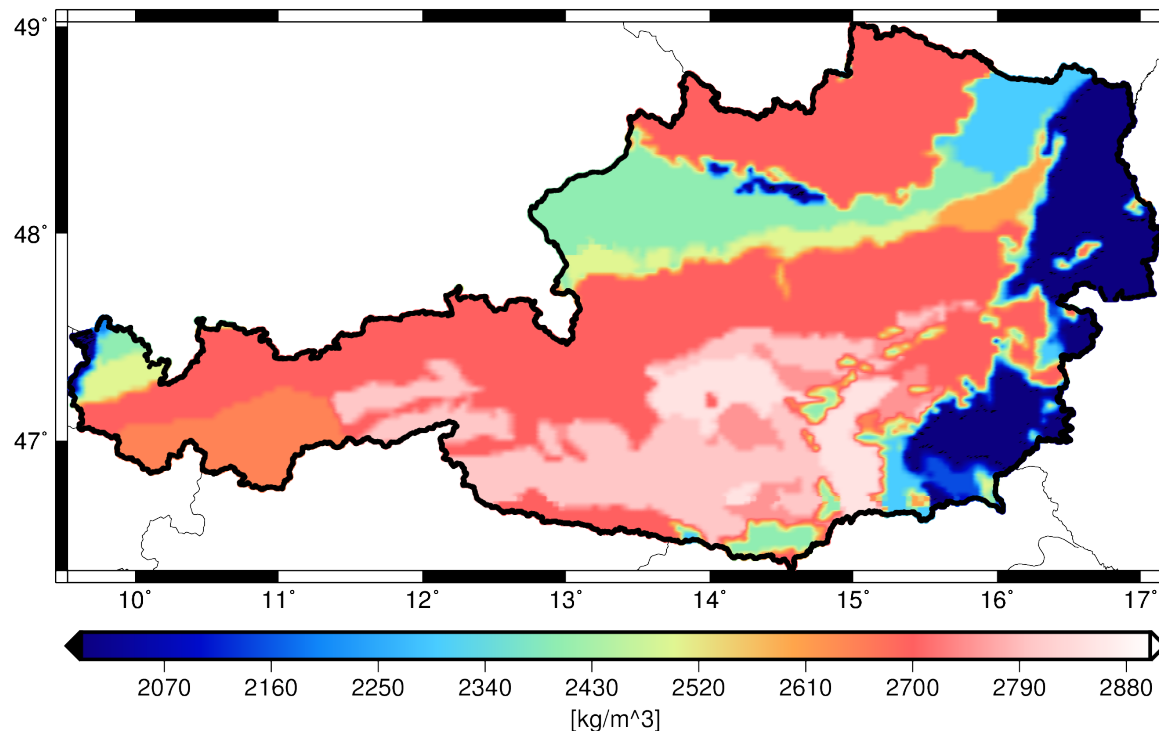
[kg/m <sup>3</sup> ]	min	max	mean
	2102.70	2870.60	2628.60



## Density Models (2)

- **Geological observations  $\rho_{geo}$ : 1 layer  $\rightarrow$  surface density model**
  - Historically grown (1950-1983), but still up to date

[kg/m <sup>3</sup> ]	min	max	mean
	2000.00	2852.00	2575.60

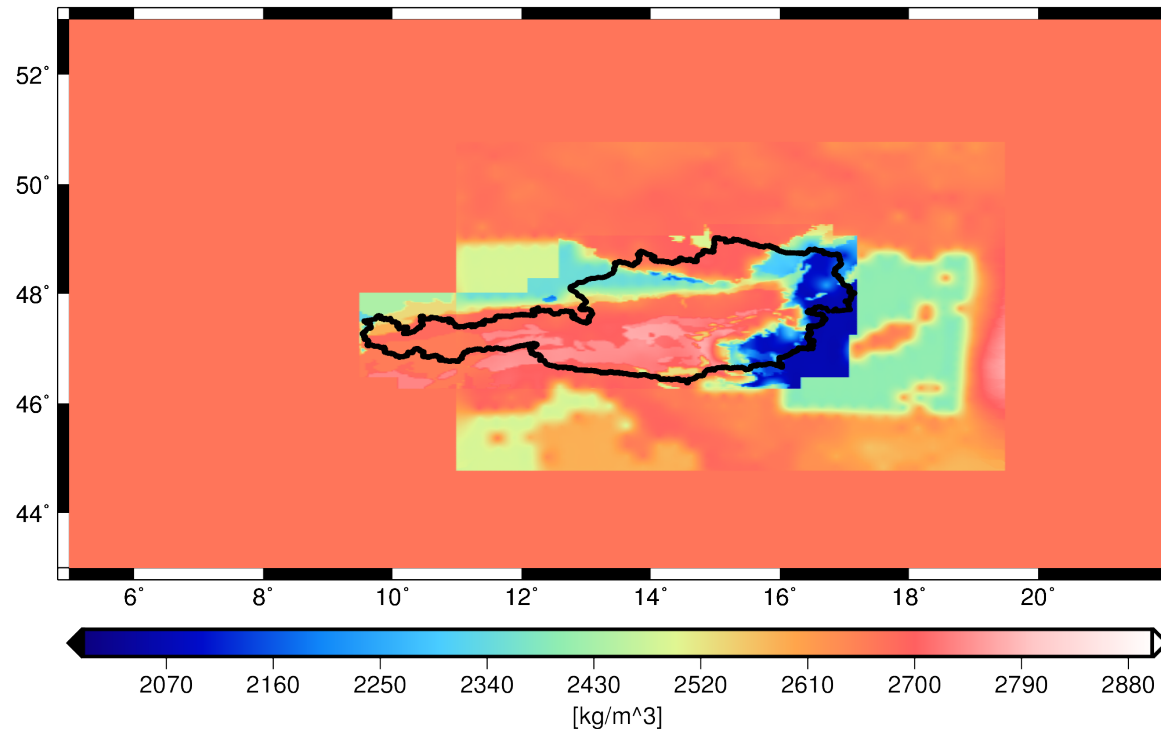


## Density Models (3)

- Hybrid model as trivial combination of both data types

$$\rho_{hyb} = \frac{\rho_{seis} + \rho_{geo}}{2}$$

[kg/m <sup>3</sup> ]	min	max	mean
	2054.34	2775.27	2651.07



## Density Models (4)

- **Three different density assumptions:**

1.) Constant standard crustal density  $\rightarrow \rho = 2670 \text{ kg/m}^3$

2.) Hybrid density model  $\rightarrow \rho_{hyb} = \frac{\rho_{seis} + \rho_{geo}}{2}$

3.) Surface density model  $\rightarrow \rho_{geo}$

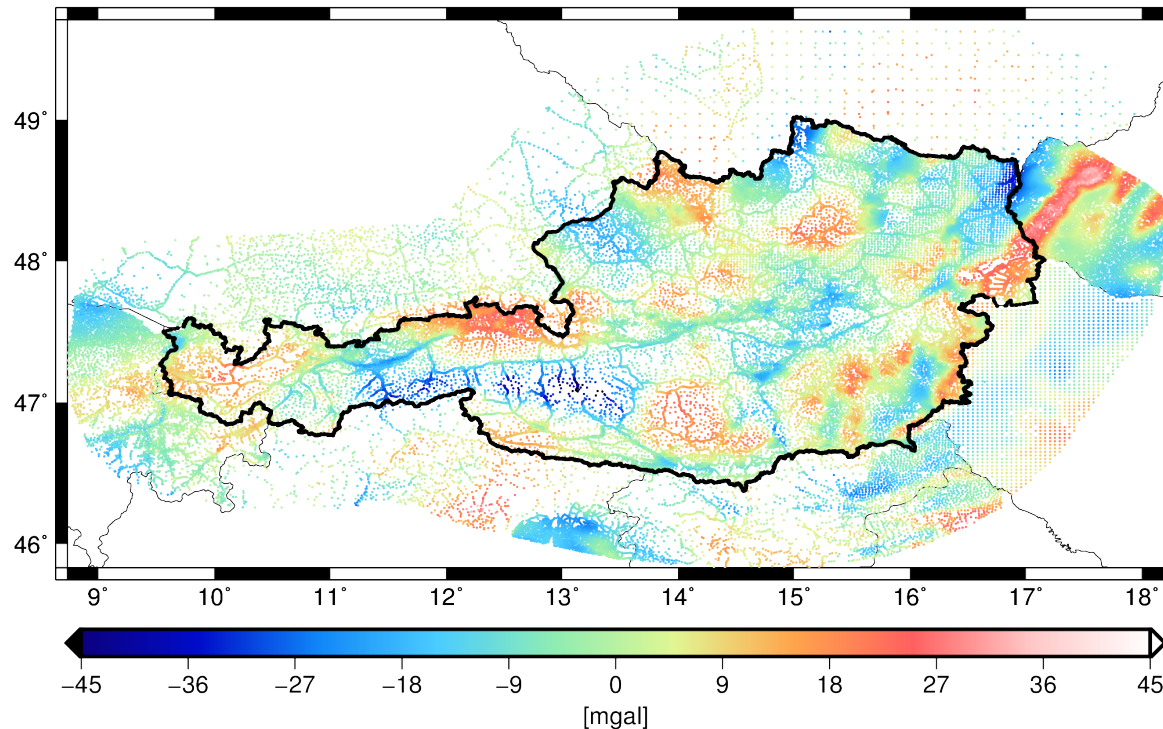
- **Questions:**

- *Significant improvements throughout the reduction step?*
- *Is any of these density models improving the geoid solution?*
- *Which density assumption performs best compared to GPS/Leveling and geopotential numbers?*

## Remove Step (1)

- **Input data:** gravity, number of data points: 72327
  - Standard crustal density  $\rho = 2670 \text{ kg/m}^3$

[mgal]	min	max	mean	rms
	-48.49	39.44	-1.10	11.70

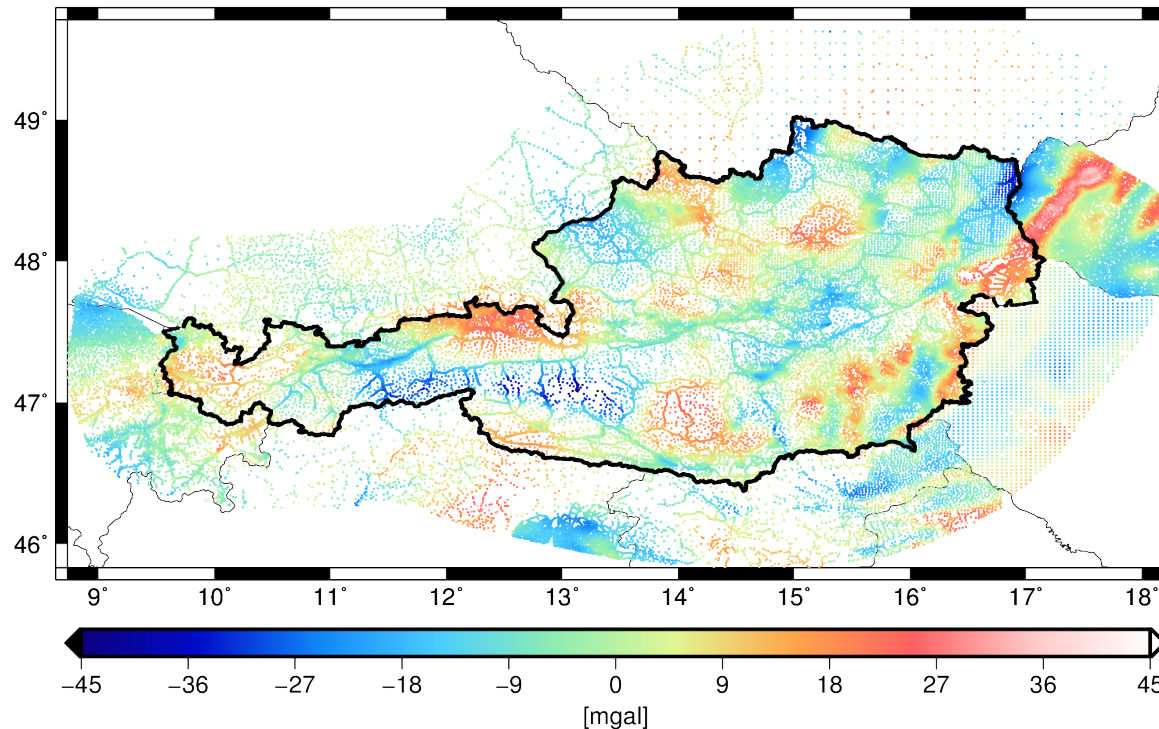


## Remove Step (2)

- **Input data:** gravity, number of data points: 72327

- Hybrid density  $\rho_{hyb} = \frac{\rho_{seis} + \rho_{geo}}{2}$

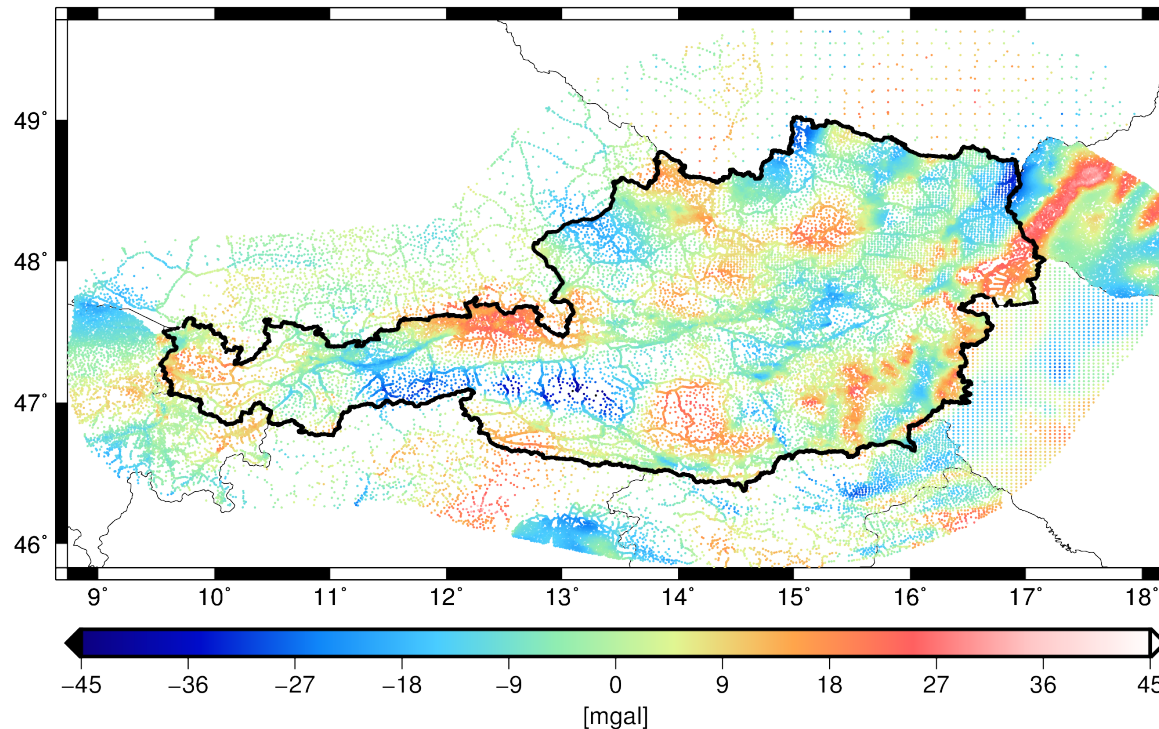
[mgal]	min	max	mean	rms
	-48.10	38.66	-1.02	11.57



## Remove Step (3)

- **Input data:** gravity, number of data points: 72327
  - Surface density  $\rho_{geo}$ , **performs best** → rms

[mgal]	min	max	mean	rms
	-49.48	37.35	-0.85	11.40

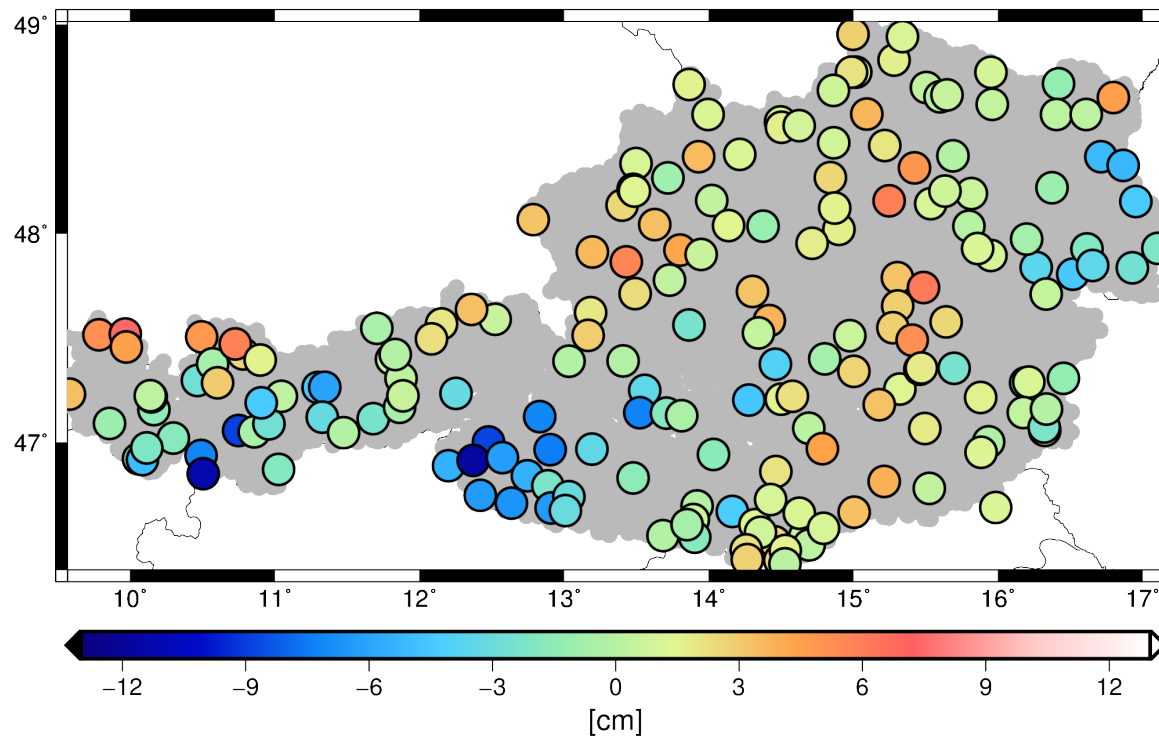


# Absolute Validation (1)

- **Geoid validation with 192 GPS/Leveling observations**

- Standard crustal density  $\rho = 2670 \text{ kg/m}^3$

[cm]	min	max	rms
	-11.68	7.43	3.33

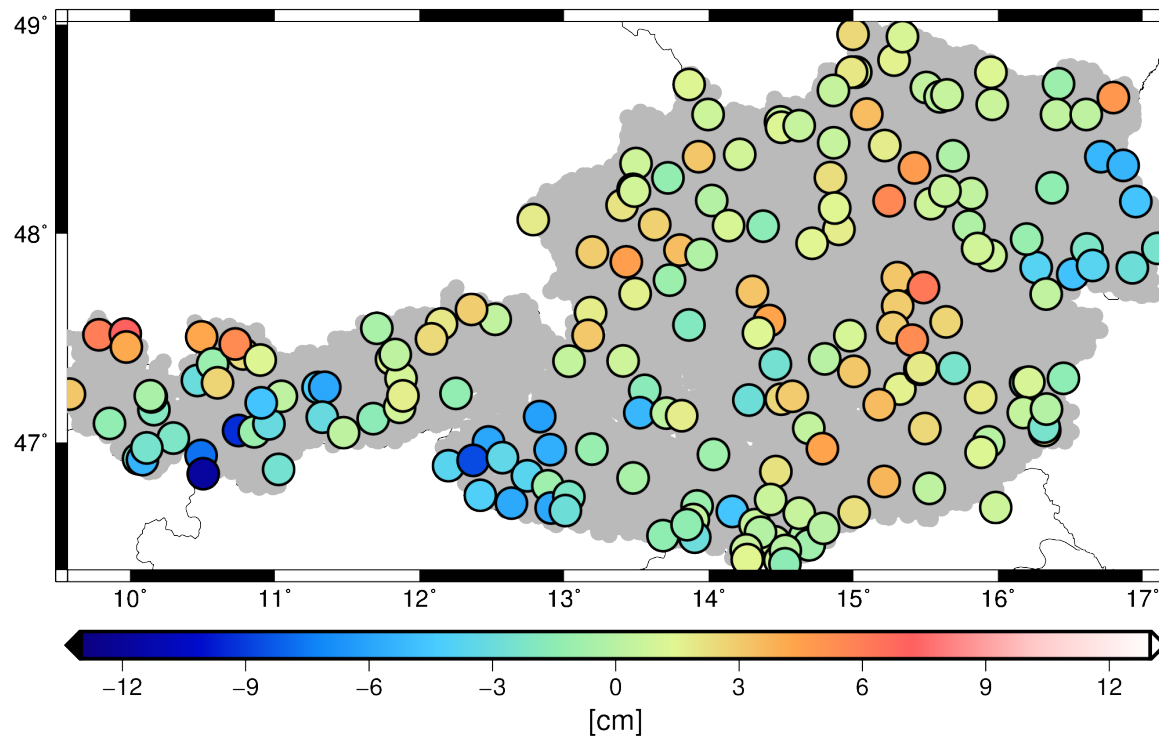


## Absolute Validation (2)

- **Geoid validation with 192 GPS/Leveling observations**

- Hybrid density model  $\rho_{hyb} = \frac{\rho_{seis} + \rho_{geo}}{2}$

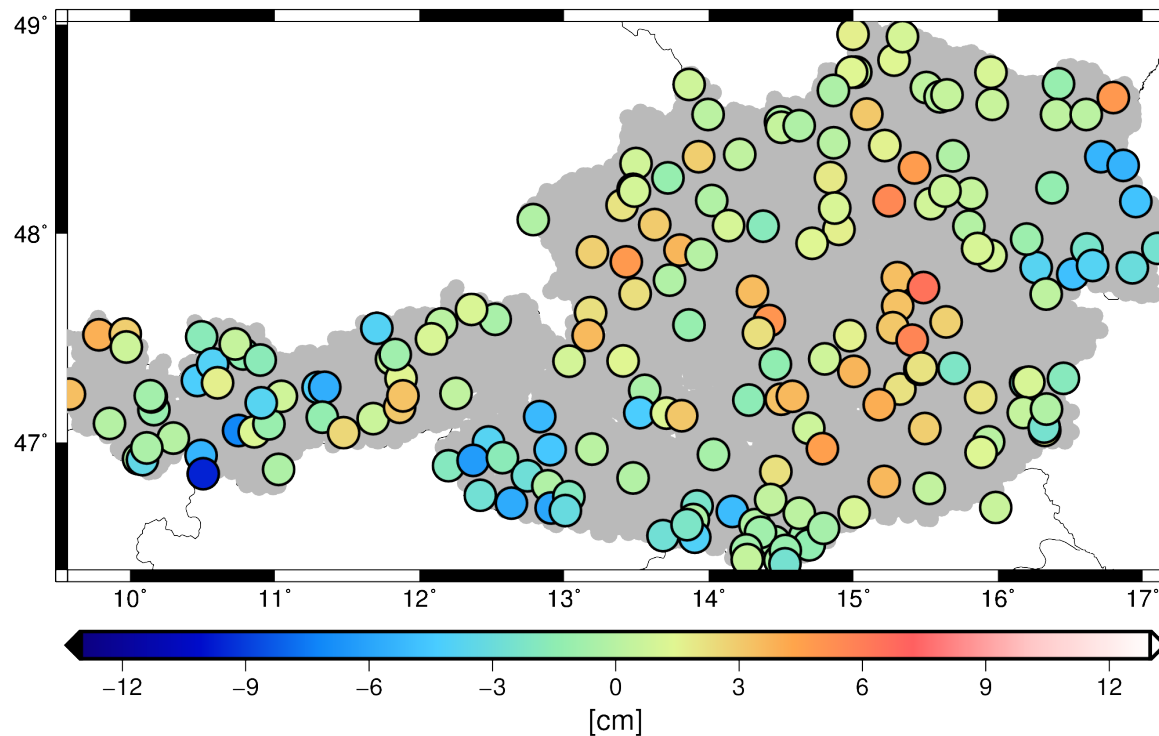
[cm]	min	max	rms
	-11.82	7.21	3.05



## Absolute Validation (3)

- Geoid validation with 192 GPS/Leveling observations
  - Surface density model  $\rho_{geo}$ , performs best  $\rightarrow$  rms

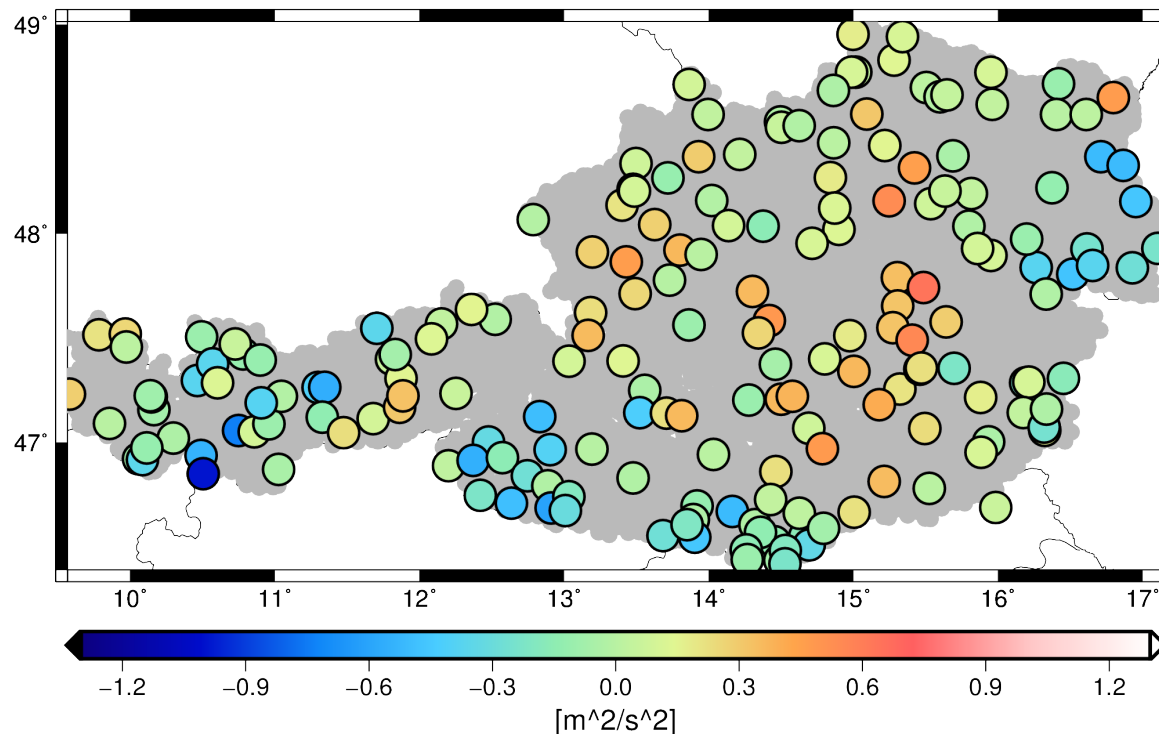
[cm]	min	max	rms
	-9.62	6.46	2.75



# Validation with Geopotential Numbers

- Validation with 192 geopotential numbers
  - Surface density model  $\rho_{geo}$ , performs best  $\rightarrow$  rms

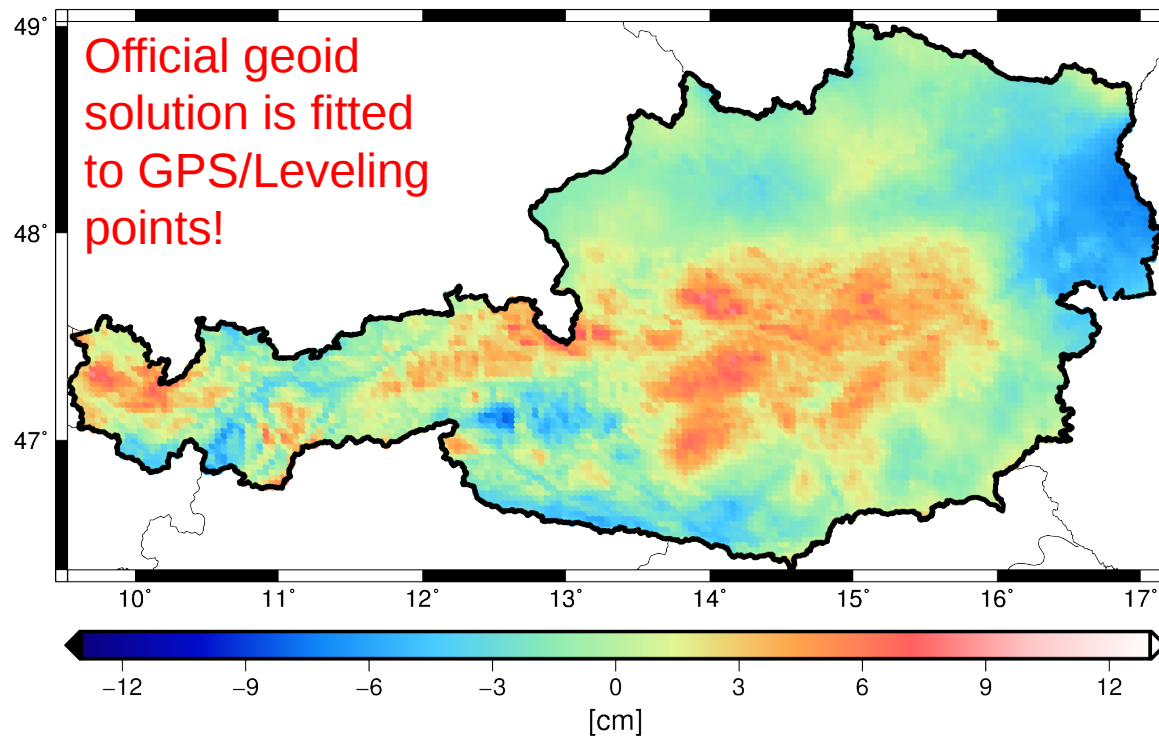
[m <sup>2</sup> /s <sup>2</sup> ]	min	max	rms
	-0.99	0.65	0.27



# Validation with Austrian Geoid Solution

- Compared to present official Austrian geoid solution → 3x3 km grid
  - Surface density model  $\rho_{geo}$

[cm]	min	max	rms
	-8.19	8.38	2.80



# Validation Gravimetric Geoid - Summary

<b>REMOVE</b>	min	max	mean	rms
Density Model	[mgal]	[mgal]	[mgal]	[mgal]
Standard	-48.49	39.44	-1.10	11.70
Hybrid	-48.10	38.66	-1.02	11.57
Surface	-49.48	37.35	-0.85	11.40

Decreasing  
rms values

<b>RESTORE</b>	min	max	rms
Density Model	[cm]	[cm]	[cm]
Standard	-11.68	7.43	3.33
Hybrid	-11.82	7.21	3.05
Surface	-9.62	6.46	2.75

Decreasing  
rms values

• **Answers:**

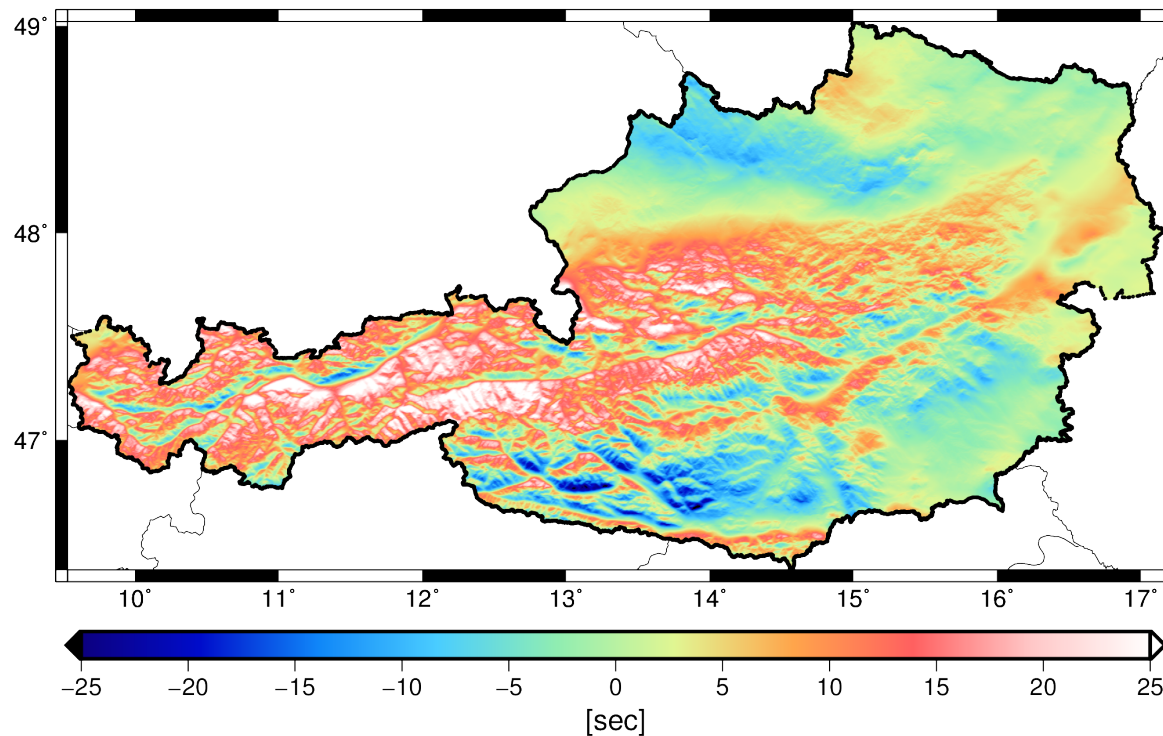
- **Significant improvements throughout the reduction step? → Yes**
- **Is any of the density models improving the geoid solution? → Yes**
- **Which density assumption performs best compared to GPS/Leveling and geopotential numbers? → Surface density**

## Further Validation with Deflections (1)

- Map of deflections of the vertical  $\rightarrow \xi$  component

- Input data: 72327 gravity points,  $\rho_{geo}$ , GOCO05s  $\rightarrow$  *quality of solution?*

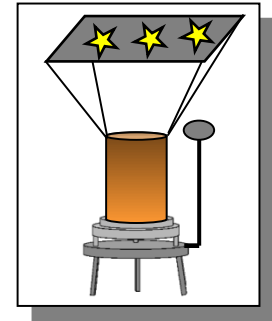
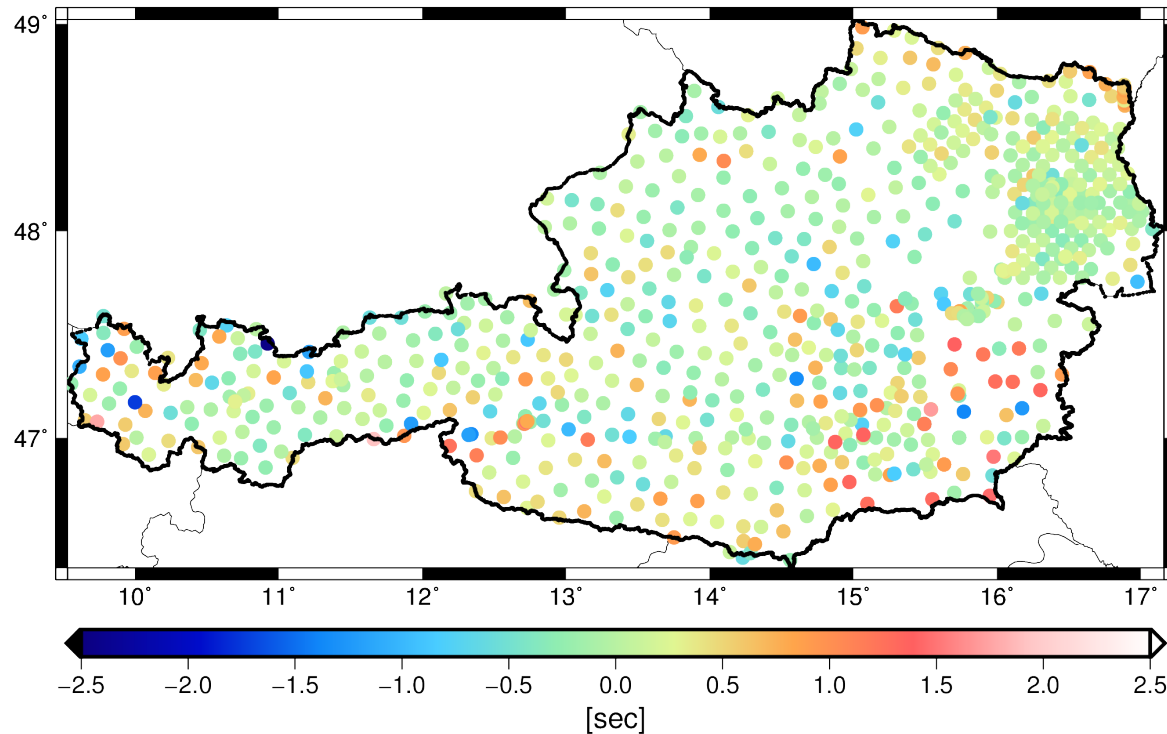
["]	min	max	mean	rms
	-26.70	39.07	3.67	8.80



## Further Validation with Deflections (2)

- Measured deflections of the vertical are used for validation
  - Validation  $\xi$  map  $\rightarrow$  735 deflections of the vertical

["]	min	max	mean	rms
	-2.44	1.91	0.08	0.49

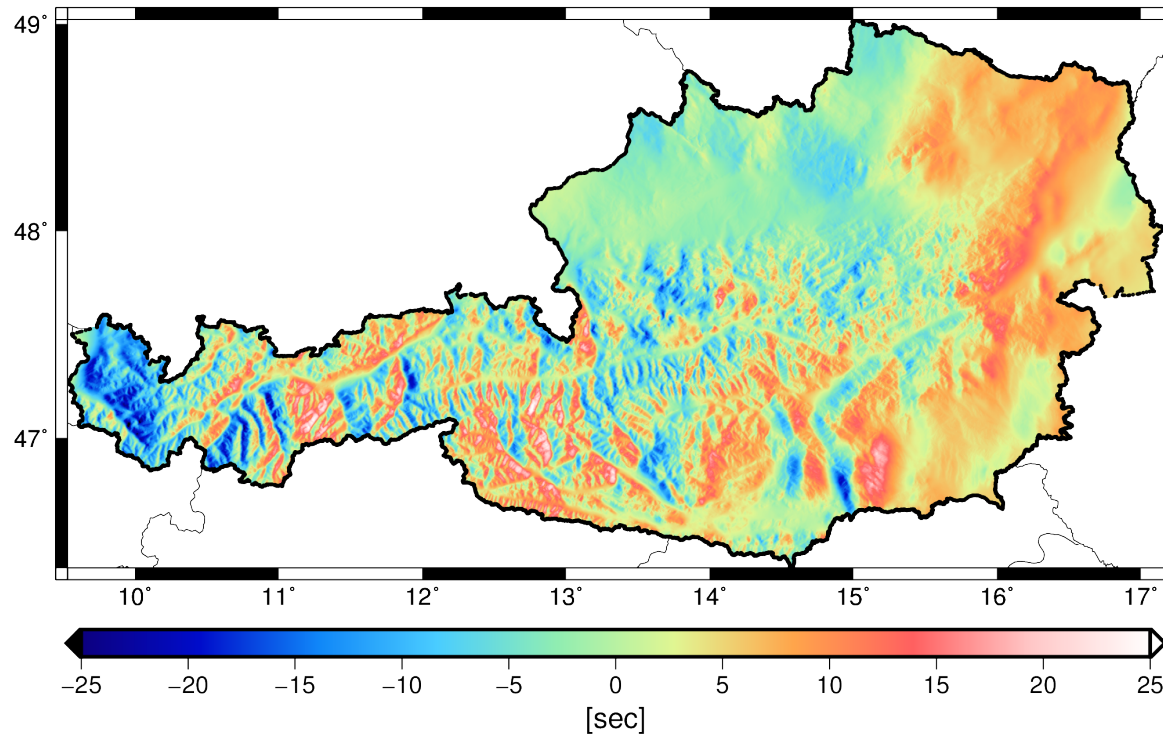


## Further Validation with Deflections (3)

- Map of deflections of the vertical  $\rightarrow \eta$  component

- Input data: 72327 gravity points,  $\rho_{geo}$ , GOCO05s  $\rightarrow$  *quality of solution?*

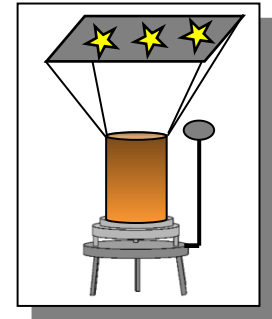
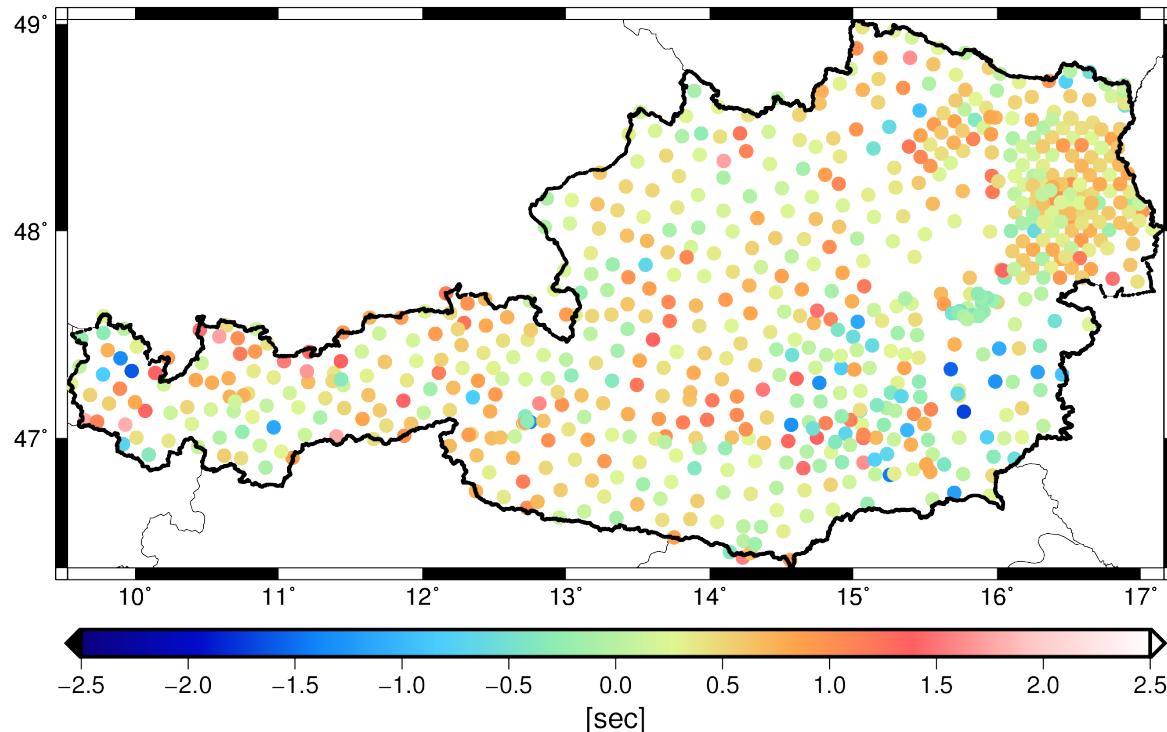
["]	min	max	mean	rms
	-27.37	26.65	1.51	6.58



## Further Validation with Deflections (4)

- Measured deflections of the vertical are used for validation
  - Validation  $\eta$  map  $\rightarrow$  735 deflections of the vertical

["]	min	max	mean	rms
	-1.71	1.80	0.35	0.63



## Summary

- **Take away messages:**

- **Density information improves** the entire **geoid computation**
- **Density models** perform **better** compared to **standard crustal density**
- **Improvements** also for **deflections of the vertical & geopotential numbers**
- **Best gravimetric geoid solution** is based on **surface density & GOCO05s**
- **Latest GOCO model** also **contributes** to an **improved geoid**

- **Problems:**

- Rms values < 3 cm possible → **Quality of 192 GPS/Leveling observations?**  
→ **Quality of density information?**

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