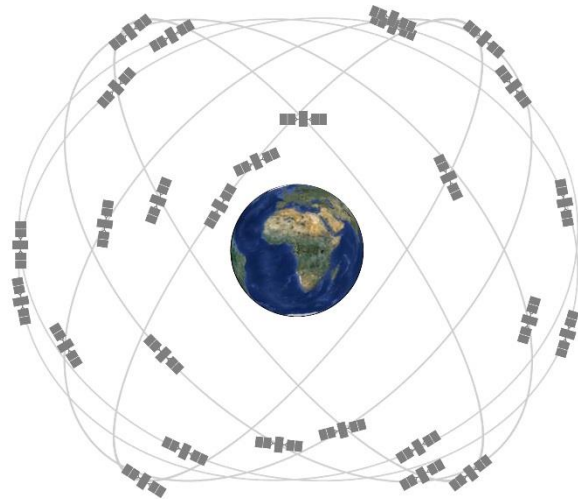


# Investigations on precise orbit modeling of GPS satellites



**Sebastian Strasser, Torsten Mayer-Gürr**

Institute of Geodesy, Graz University of Technology  
WG Theoretical Geodesy and Satellite Geodesy

Geodetic Week 2015, Stuttgart, Germany

# Introduction

Bachelor thesis on the effects of solar radiation pressure on GPS orbits

## Student Project Assistant

- Funded by the Austrian Research Promotion Agency (FFG)
- Main focus: GPS orbit modeling and orbit determination

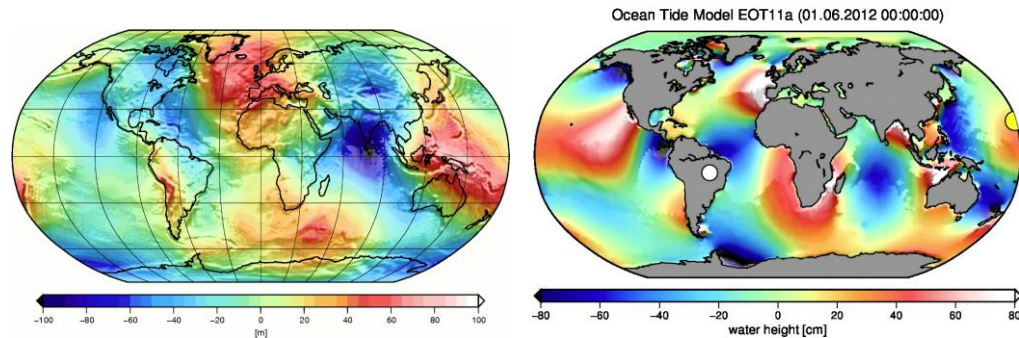


Planned: Master thesis on precise orbit determination of GPS satellites

# Investigated effects and models

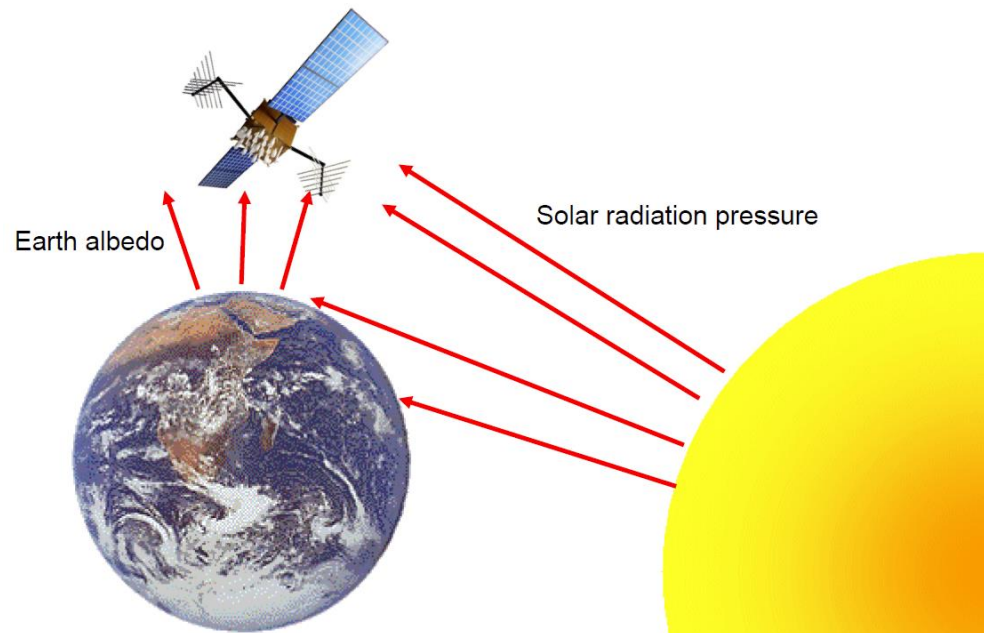
## Conservative forces

- Gravity field model
- Ocean tides
- Global mass variations
- Pole tides and ocean pole tides



## Non-conservative forces

- Solar radiation pressure
- Earth albedo
- Antenna thrust



# Investigation approach

## Numerical orbit integration using variational equations

- Orbit modeling only, no GPS observations involved

## Estimation of parameters required for best fit to daily IGS final orbits

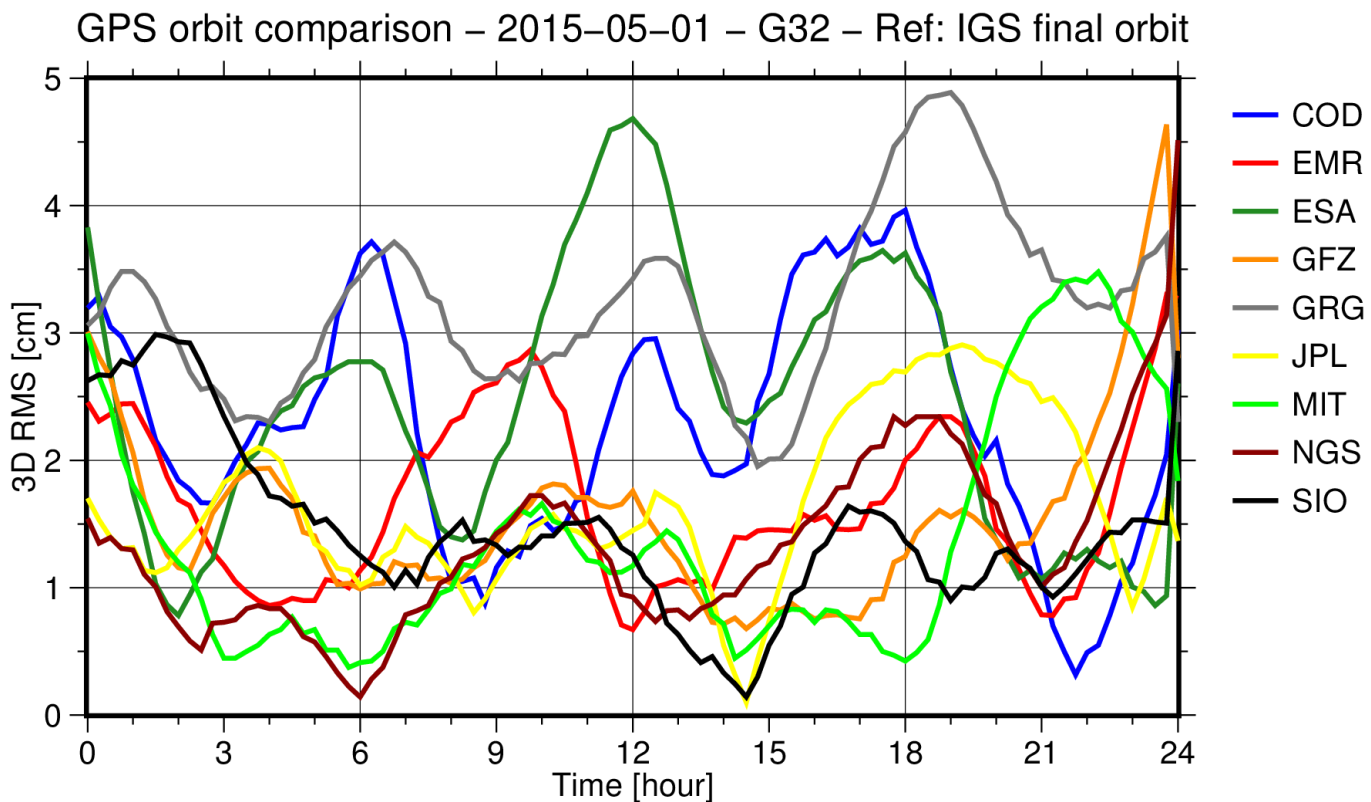
- Initial state vector (position, velocity)
- Solar radiation pressure parameters

## Comparison approach

- Multiple solutions with investigated model enabled vs. disabled
- Multiple solutions with different models for investigated effect, if applicable
- Difference of the solutions as 3D RMS per epoch (60 sec. sampling)

# IGS final orbits

Combination of orbits from 9 IGS analysis centers



Stated accuracy: 1D mean RMS: ~2.5 cm

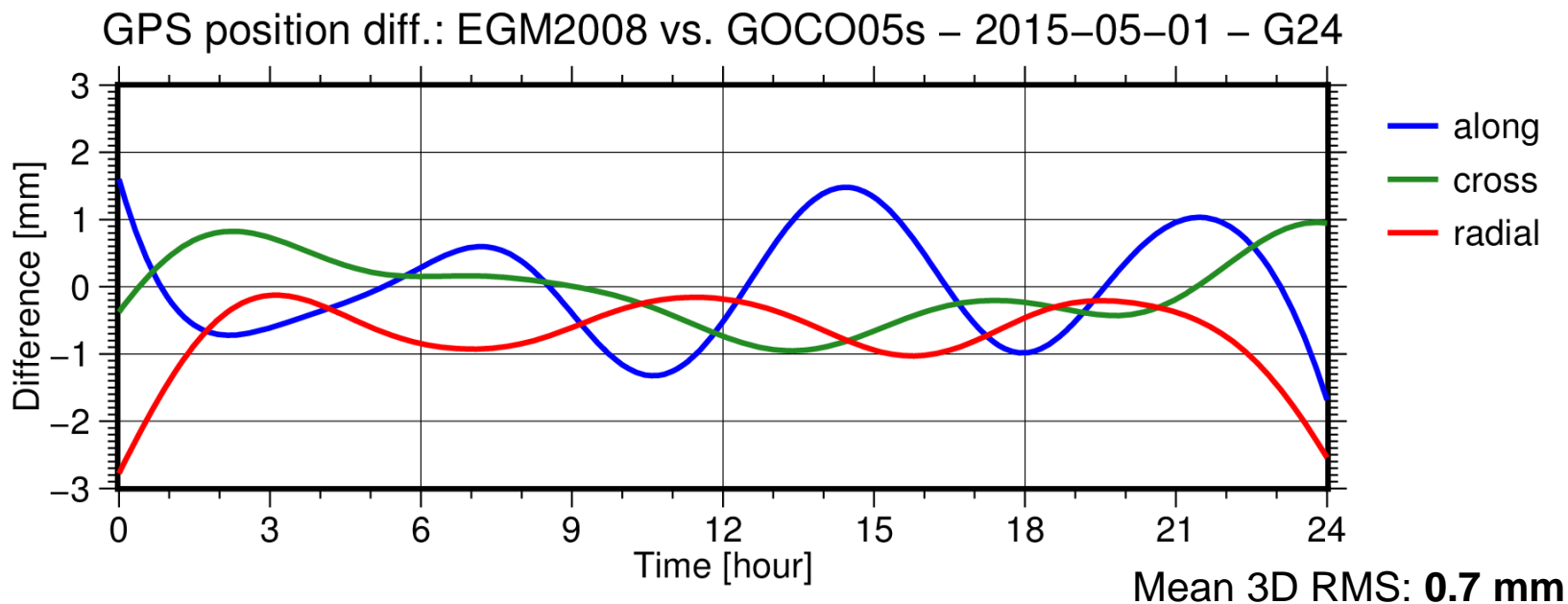
# Conservative forces

# Gravity field model selection

Current IGS recommendation: EGM2008

Most recent model: GOCO05s

- Published in April 2015
- Contains data from GOCE, GRACE, kinematic orbits, SLR



# Gravity field model selection

## EGM2008

- Max. degree 2190
- Satellite and terrestrial data

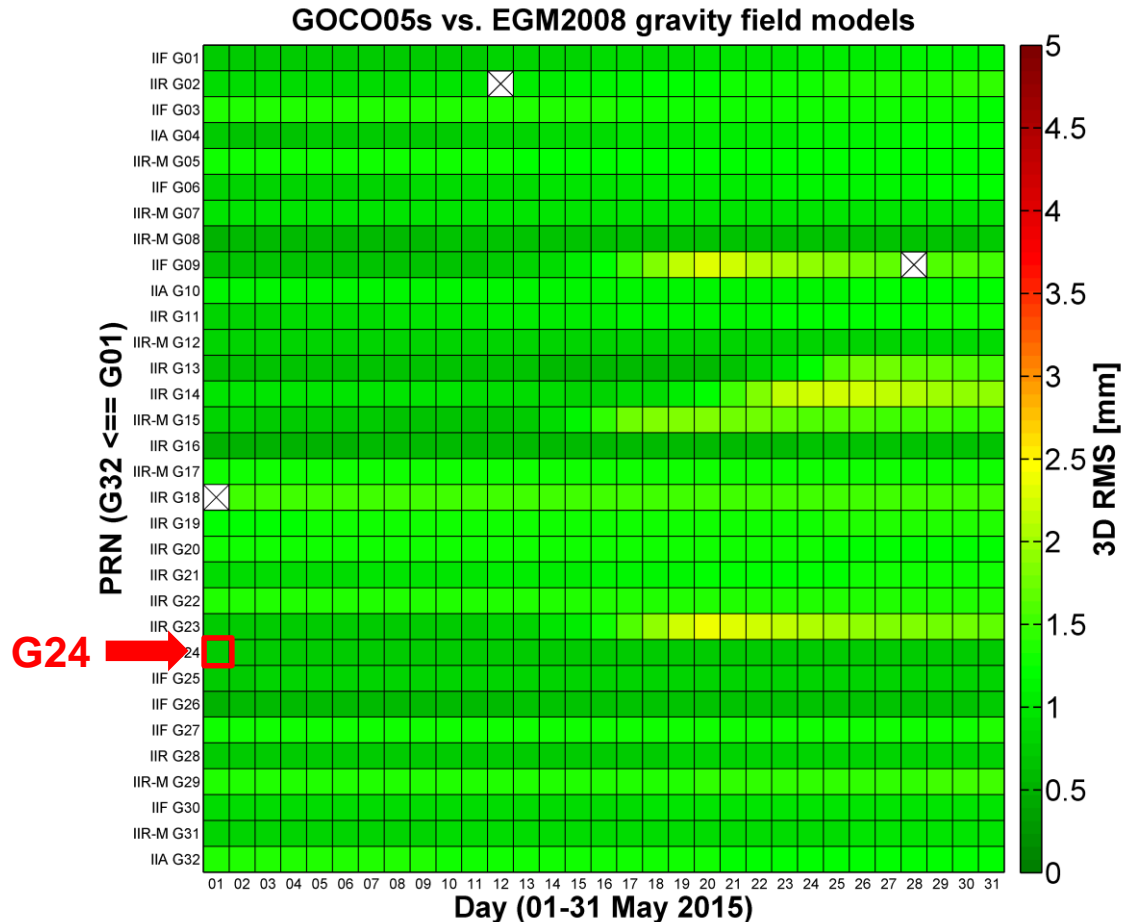
## GOCO05s

- Max. degree 280
- Satellite data only
- Higher accuracy at low degrees

Max. degree 10 sufficient for GPS due to high altitude

## EGM2008 vs. GOCO05s

- May 2015 mean 3D RMS: **1.0 mm** → EGM2008 sufficient, GOCO05s recommended





# Ocean tide models

## EOT11a

- Empirical Ocean Tide model
- DGFI, Germany

## FES2004

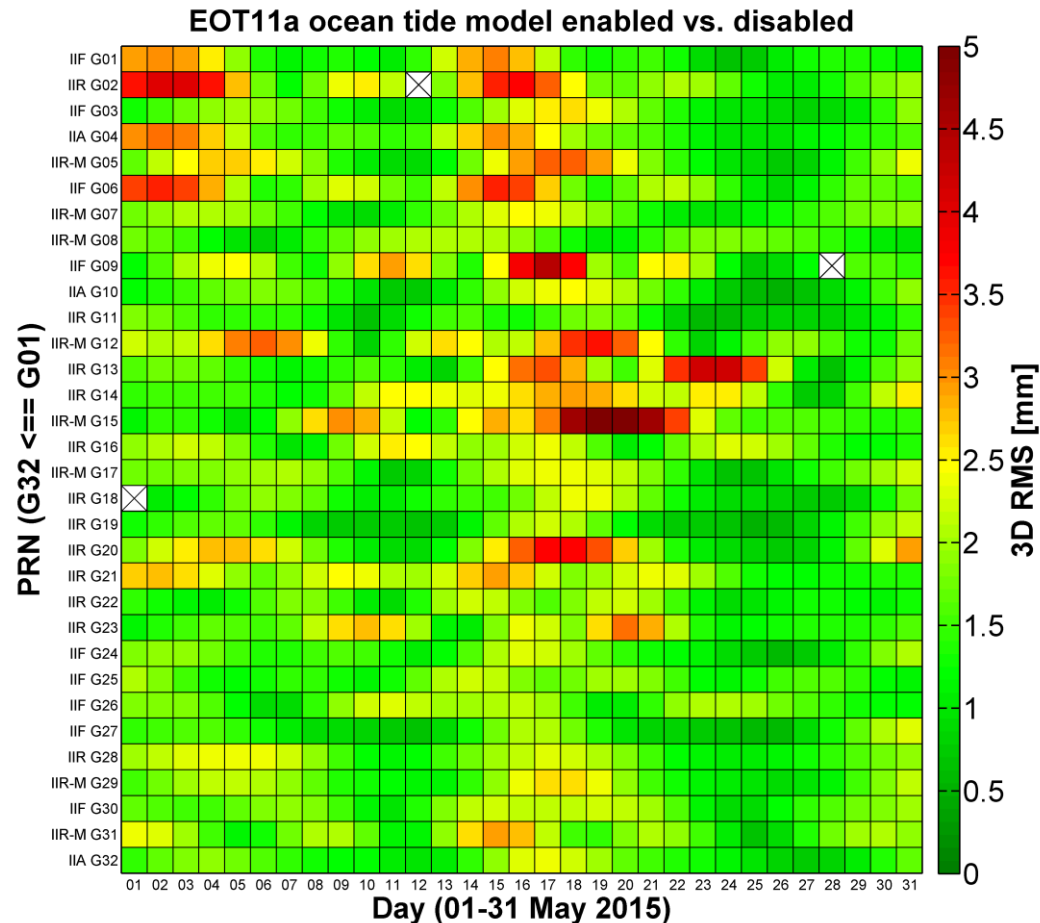
- Finite Element Solutions
- CLS/CNES/LEGOS, France

## EOT11a enabled vs. disabled

- May 2015 mean 3D RMS: **1.7 mm**

## EOT11a vs. FES2004

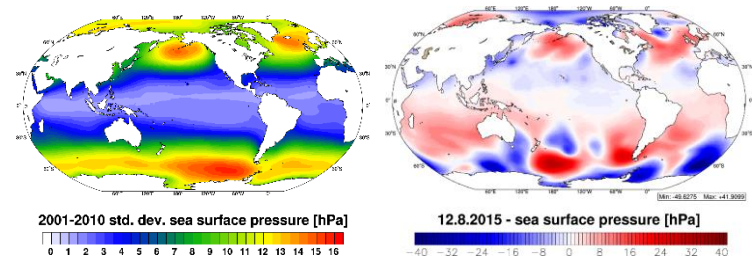
- May 2015 mean 3D RMS: **0.0 mm** → Use of an ocean tide model recommended  
No difference between models



# Mass variations, pole tides and ocean pole tides

## AOD1B mass variation model

- Atmosphere and Ocean De-aliasing Level-1B
- GFZ, Germany

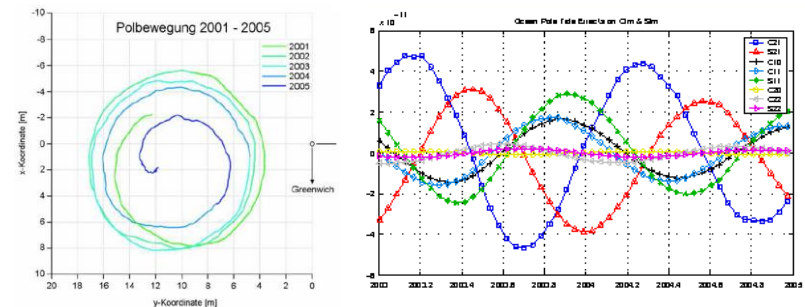


## AOD1B enabled vs. disabled

- May 2015 mean 3D RMS: **0.3 mm** → Consideration of mass variations not required

## Pole tides and ocean pole tides

- Pole tide model: IERS 2010
- Ocean pole tide model: Desai (2004)



## Pole tides and ocean pole tides enabled vs. disabled

- May 2015 mean 3D RMS: **0.3 mm** → Pole tides and ocean pole tides can be neglected

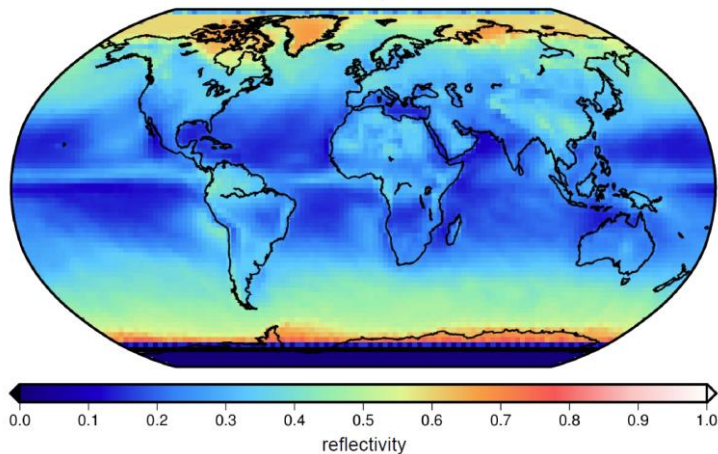
# Non-conservative forces

# Earth albedo

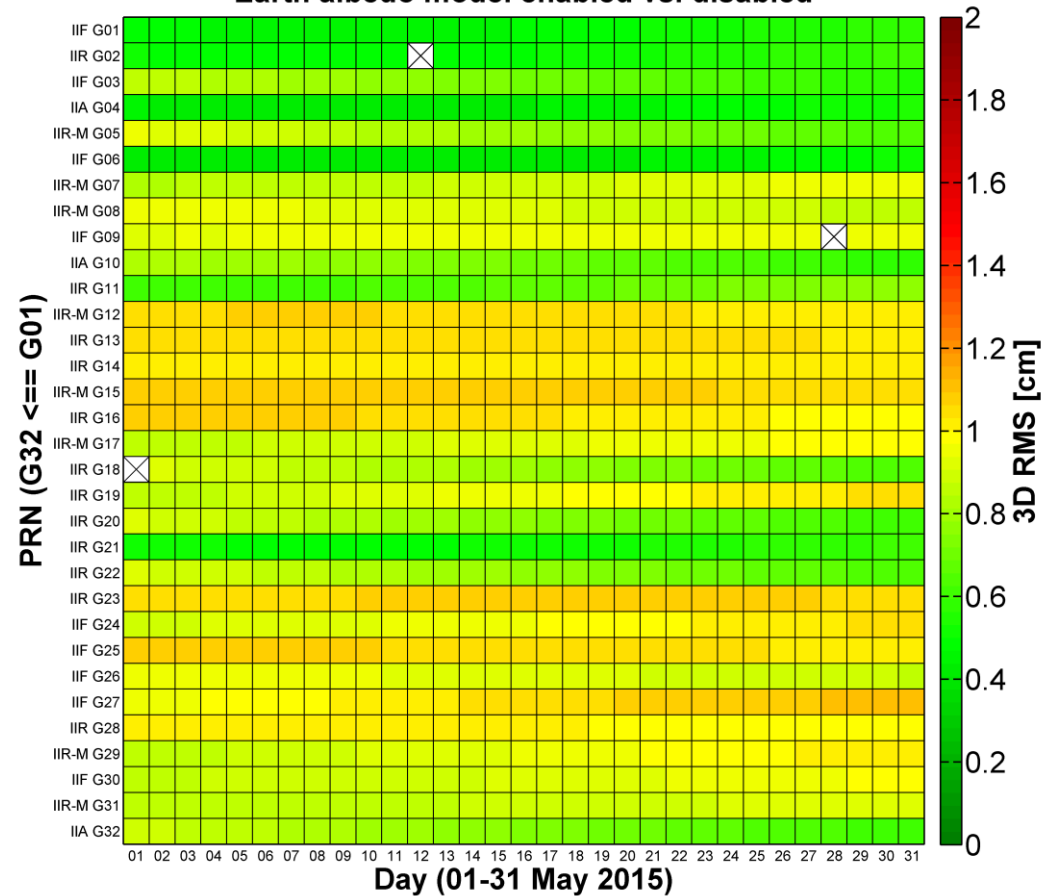
Box-wing model by Rodriguez-Solano et al. (2011)

Based on CERES data

CERES (Clouds and the Earth's Radiant Energy System) data  
May



Earth albedo model enabled vs. disabled



Earth albedo enabled vs. disabled

- May 2015 mean 3D RMS: **0.8 cm** → Use of box-wing albedo model recommended

# Solar radiation pressure

A priori box-wing model based on Rodriguez-Solano et al. (2011)

- A priori model only currently not sufficient

## Extended CODE Orbit Model

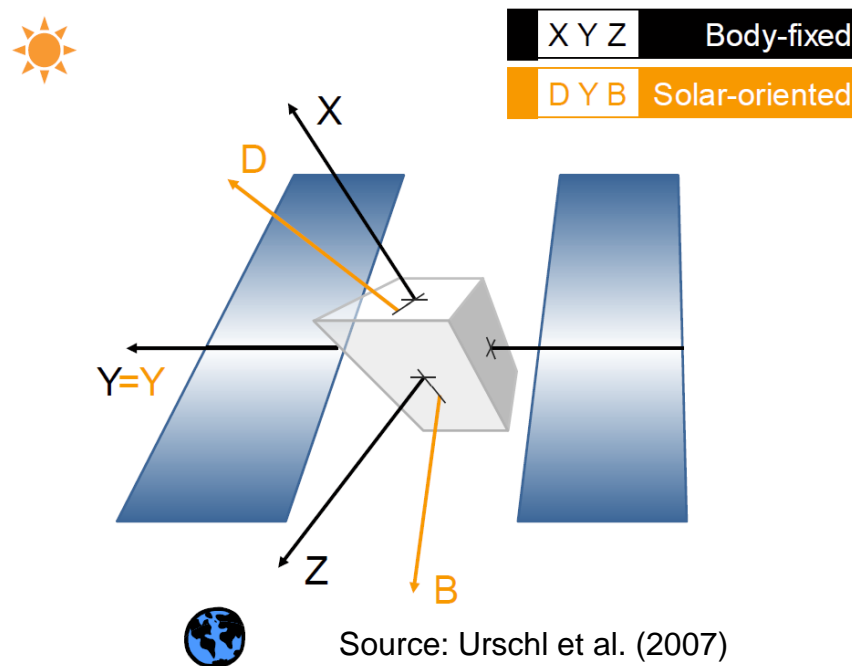
- Constant terms:  $D_0, Y_0, B_0$
- 1 per revolution terms:  $D_c, D_s, Y_c, Y_s, B_c, B_s$

## Update from CODE in January 2015

- 2 per revolution terms:  $D_{c2}, D_{s2}$
- 4 per revolution terms:  $D_{c4}, D_{s4}$

$$\mathbf{a}_{SRP} = D(\Delta u) \mathbf{e}_D + Y(\Delta u) \mathbf{e}_Y + B(\Delta u) \mathbf{e}_B$$

$$D(\Delta u) = D_0 + D_c \cos(\Delta u) + D_s \sin(\Delta u) + D_{c2} \cos(2 \Delta u) + D_{s2} \sin(2 \Delta u) + \dots$$

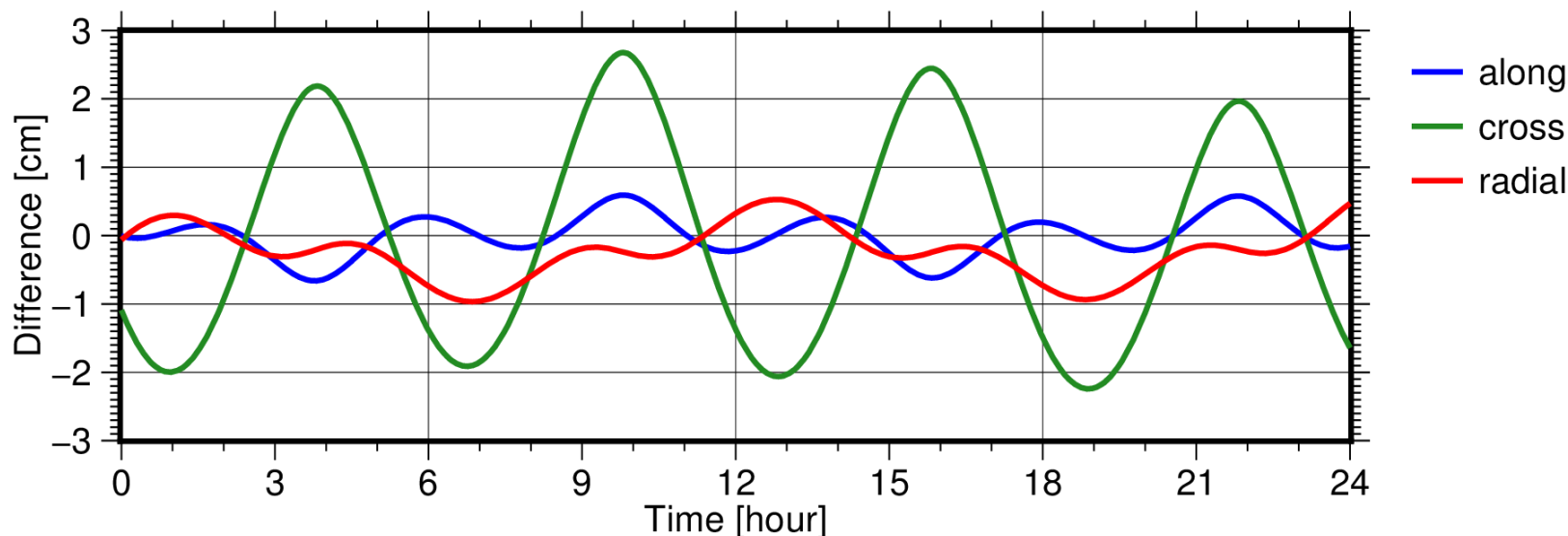


# Solar radiation pressure

## ECOM 5 parameters

- Constant terms:  $D_0, Y_0, B_0$
- 1 per revolution terms:  $B_c, B_s$

GPS position diff.: ECOM5 vs. ECOM5 + box-wing model – 2015-05-01 – G01



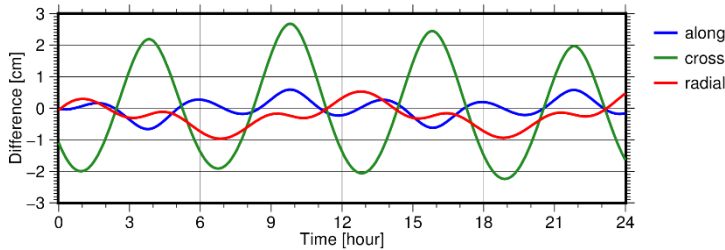
Significant 2 per revolution effects modeled by a priori box-wing model

# Solar radiation pressure

## ECOM 5 parameters

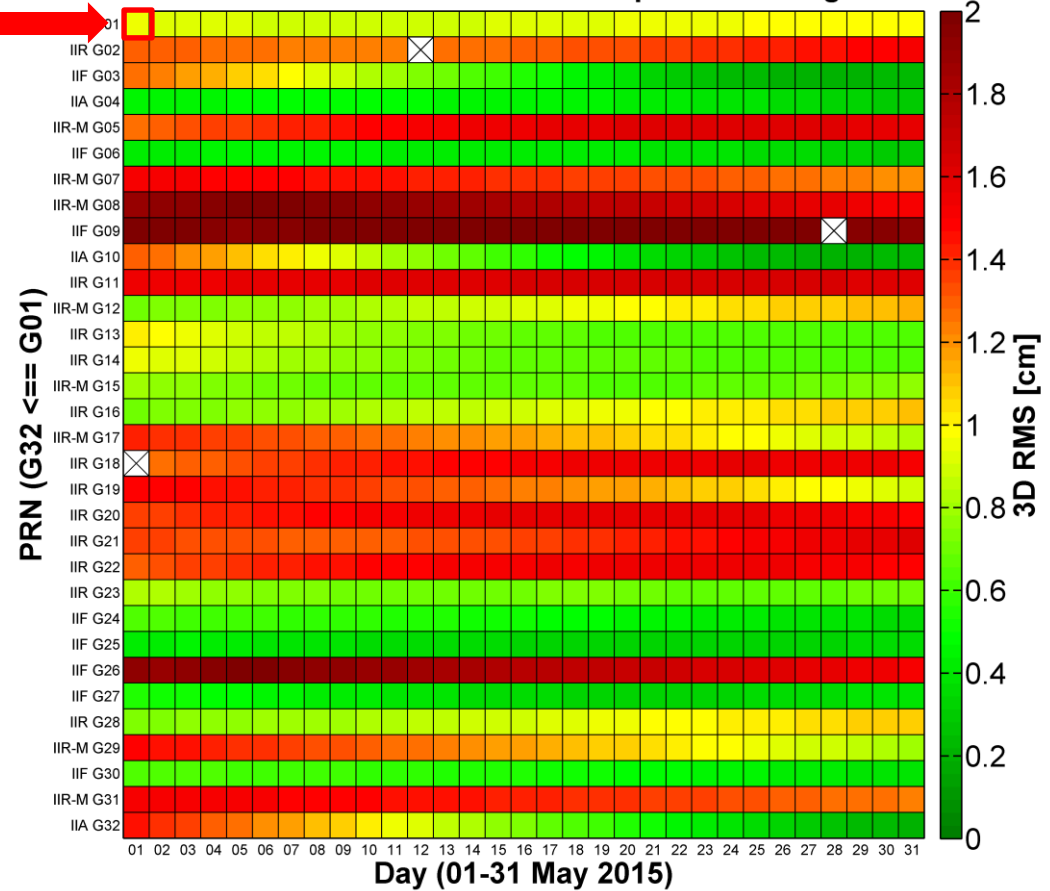
- Constant terms:  $D_0, Y_0, B_0$
- 1 per revolution terms:  $B_c, B_s$

GPS position diff.: ECOM5 vs. ECOM5 + box-wing model – 2015-05-01 – G01



**G01**

ECOM5 vs. ECOM5 combined with a priori boxwing model



## ECOM5 vs. ECOM5 + box-wing

- May 2015 mean 3D RMS: **1.0 cm** → Significant effects not caught by ECOM5 only

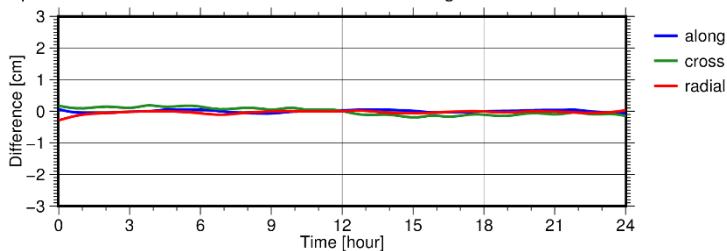
# Solar radiation pressure

## ECOM 9 parameters (new)

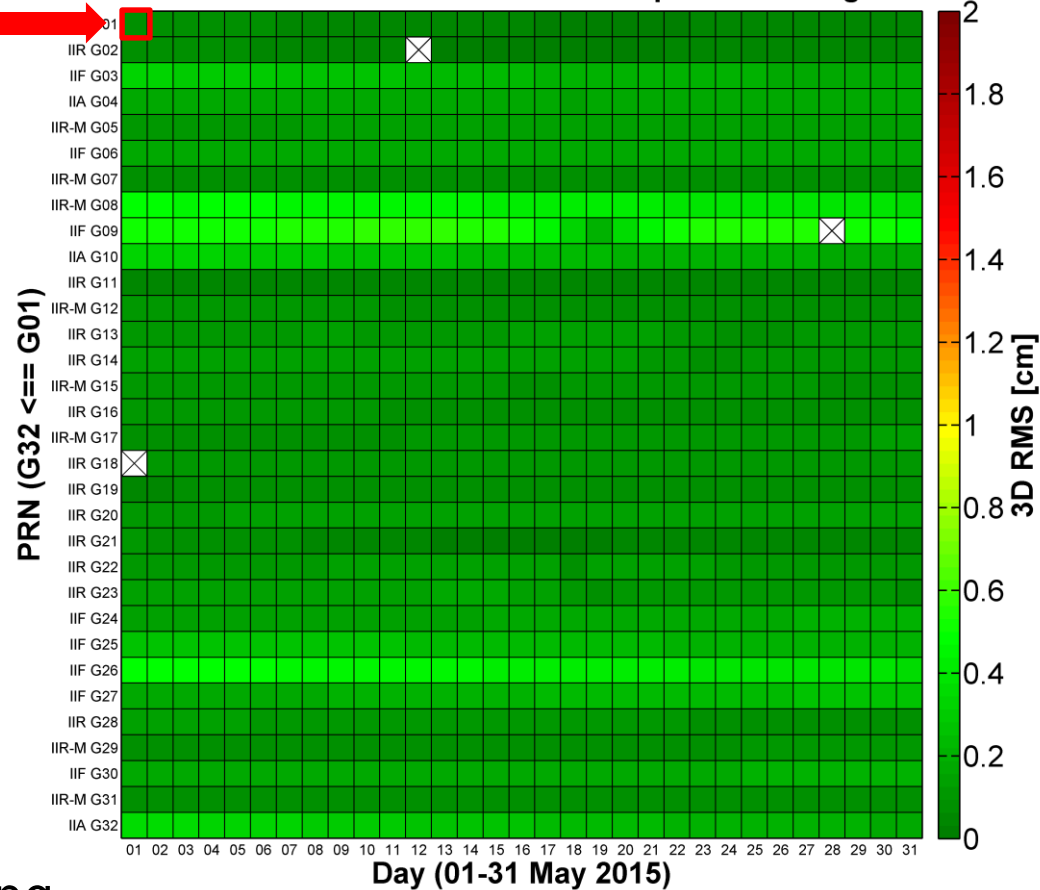
- Constant terms:  $D_0, Y_0, B_0$
- 1 per revolution terms:  $B_c, B_s$
- 2 per revolution terms:  $D_{c2}, D_{s2}$
- 4 per revolution terms:  $D_{c4}, D_{s4}$

**G01**

GPS position diff.: ECOM9N vs. ECOM9N + box-wing model – 2015-05-01 – G01



ECOM9N vs. ECOM9N combined with a priori boxwing model



## ECOM9N vs. ECOM9N + box-wing

- May 2015 mean 3D RMS: **0.2 cm** → Most effects caught by ECOM9N only



# Antenna thrust

Transmission of GPS signals towards +Z axis (Earth)

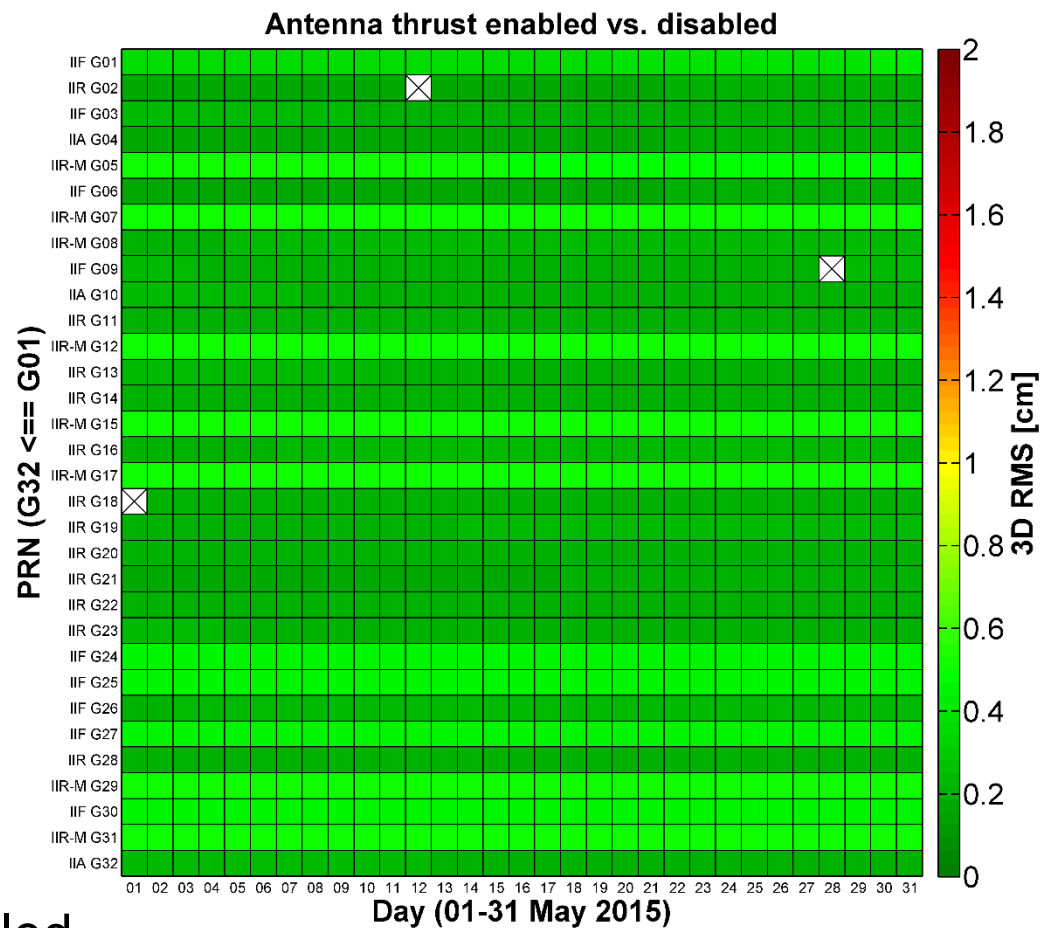
Block-dependent trans. power (new signals with IIR-M, IIF)

IGS model values

- IIA: 76 W
- IIR: 85 W
- IIR-M: 108 W (no M) / 198 W
- IIF: 154 W (no M) / 249 W

Antenna thrust enabled vs. disabled

- May 2015 mean 3D RMS: **0.3 cm** → Use of antenna thrust model recommended



# Conclusion

## Conservative forces

Gravity field model	EGM2008 sufficient, GOCO05s recommended
Ocean tides	Any current model recommended
Global mass variations	Neglectable
Pole tides and ocean pole tides	Neglectable

## Non-conservative forces

Solar radiation pressure	Currently not modeled sufficiently by a priori box-wing model Estimation of 2 per revolution terms recommended (ECOM9N)
Earth albedo	Box-wing model recommended
Antenna thrust	Modeling recommended

**Thank you for your attention!**