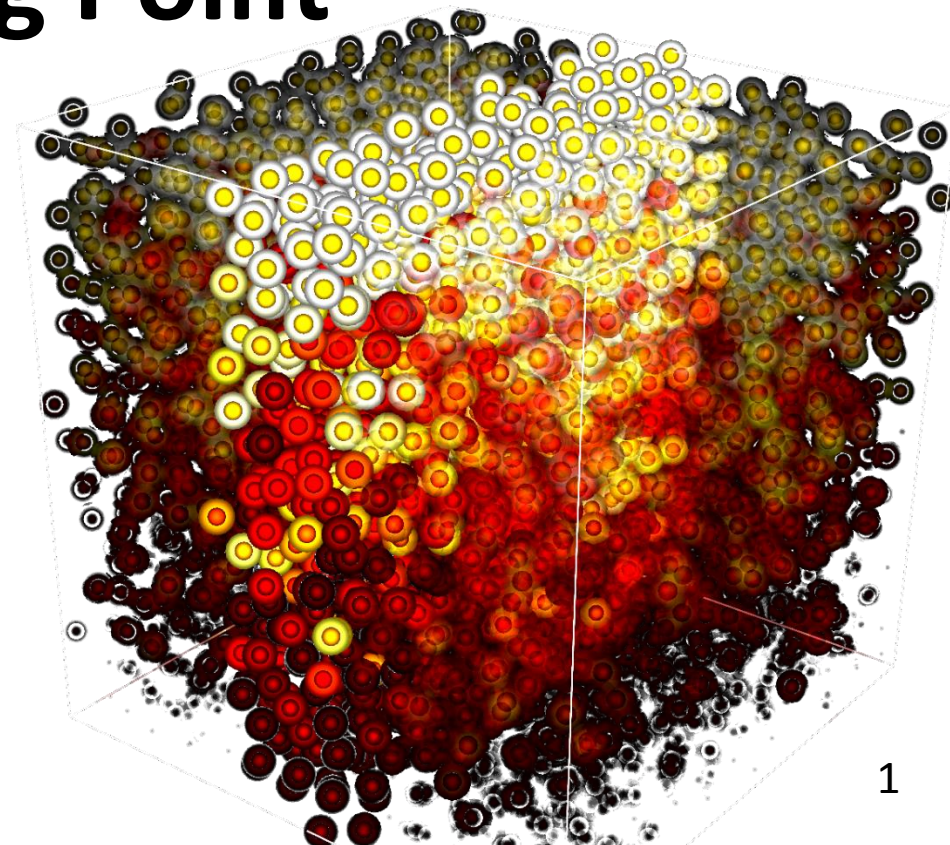


# Thermal Fluxes in Wall Bounded Sheared Granular Beds Near the Jamming Point

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Austria

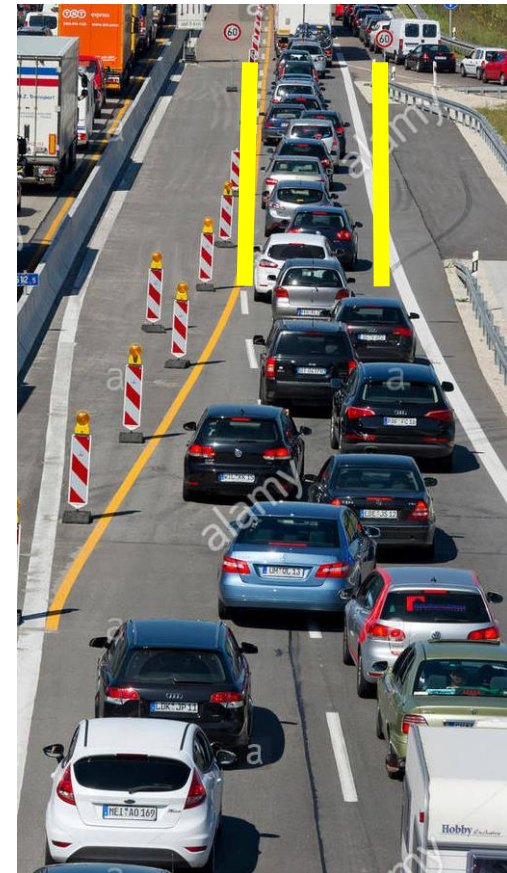


# Introduction

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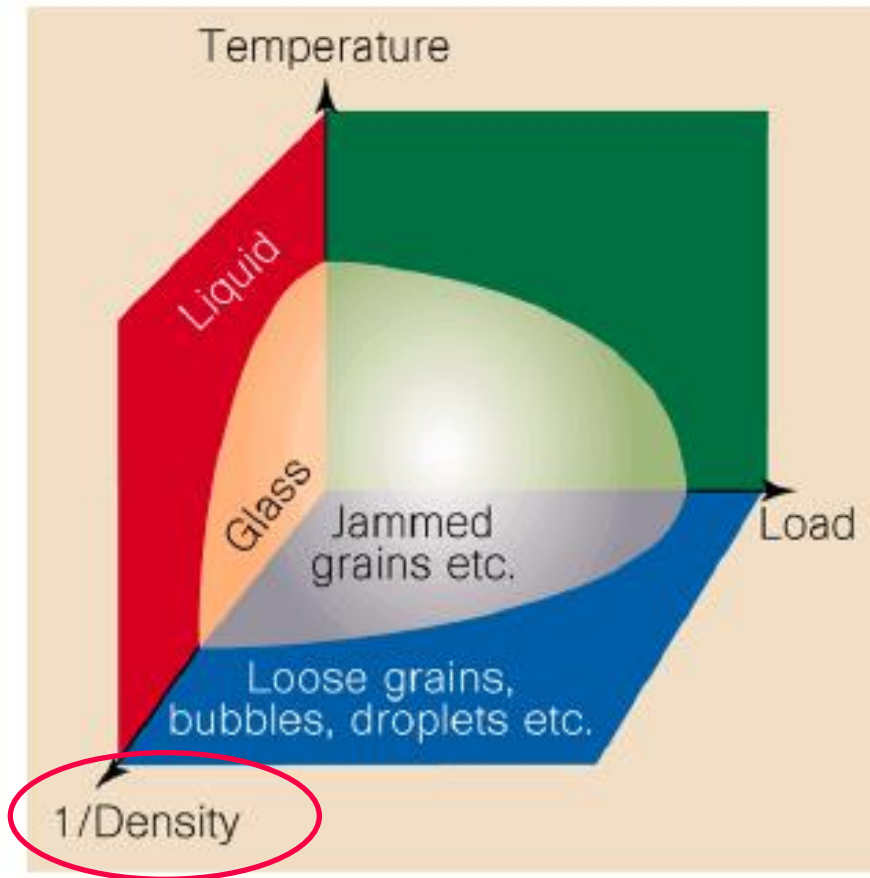
*“Jamming occurs when a system develops a yield stress—behaves as a solid—in a disordered state.”* (Liu Research Group webpage)

- Stress relaxation time of a system exceeds a certain value
- Can be found in many applications as
  - Supercooled liquids
  - Glass
  - Foams and emulsions
  - **Granular materials**
- Granular material at high packing density relevant for **reactors, geomechanics**, etc.
- Thus, effect of jamming on **local particle temperature** is interesting

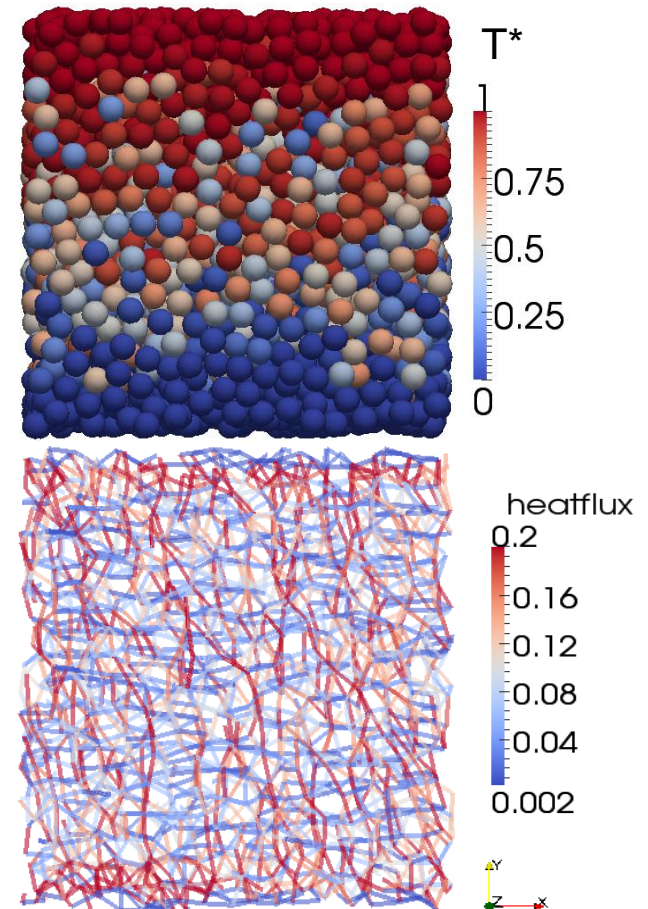


# Introduction

## Jamming Point Diagram<sup>1</sup>



## Local Particle Temperature? Effective Heat Conductivity?<sup>2</sup>



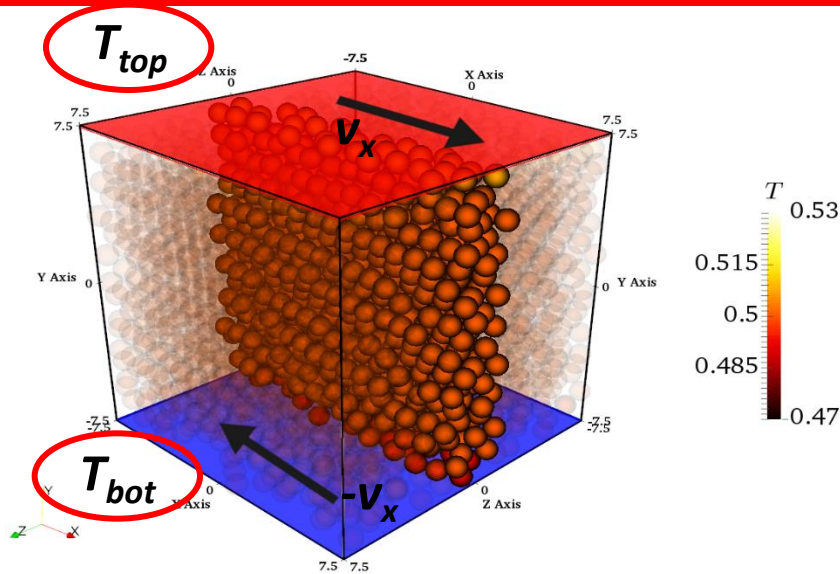
<sup>1</sup>A. J. Liu and S. R. Nagel, *Nature* 396, N6706, 21 (1998)

<sup>2</sup>Mohan et al. (2013), *Fluidization XIV*

# Simulation Method



# Simulation Method



- Deformation of box with **constant wall velocity**, periodic BC
- Parameter dependency:
  - **Biot number**
  - Wall velocity (shear rate)
  - **Volume fraction**
  - Particle conductivity
- **Thermal fluxes** are simulation result

Biot number

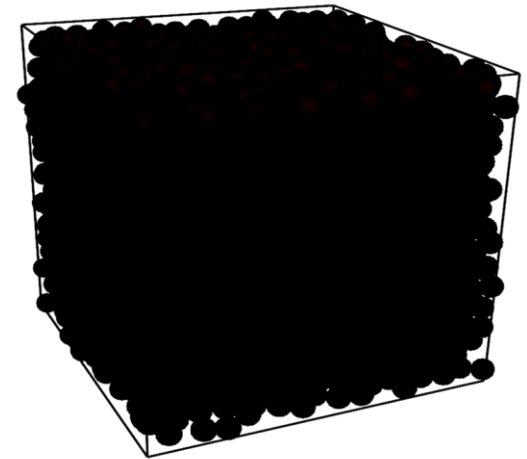
$$Bi = \frac{\alpha d_p}{\lambda_p}$$

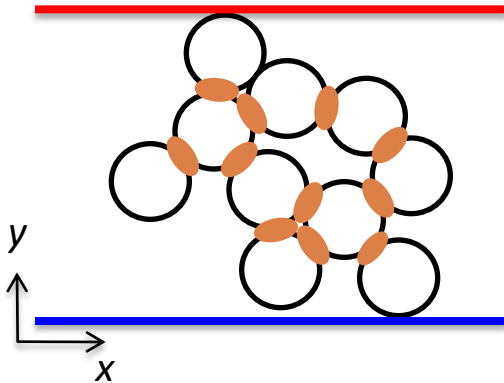
$$\dot{\gamma} = \gamma d_p^{3/2} / \sqrt{k_n / \rho_f}$$

Dimensionless shear rate

Peclet number

$$Pe = \frac{(d_p/2)^2}{\lambda_p / (\rho_p c_p)} \gamma$$



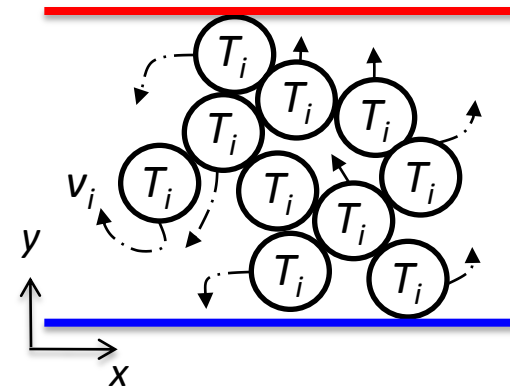


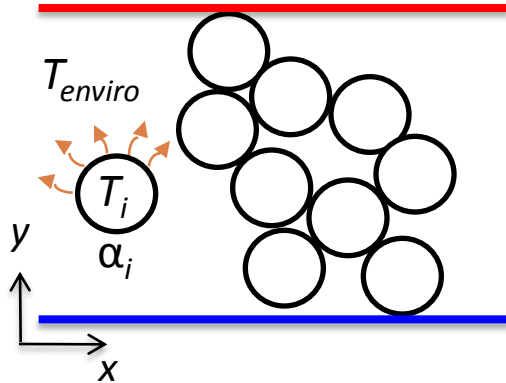
- **Conduction** due to particle-particle contact

$$\mathbf{q}^{cond} = \frac{1}{V} \sum_{co} 2 \lambda_P A_{co}^{1/2} (T_i - T_j) \mathbf{r}_{ij}$$

- (Granular) **Convection** due to individual particle motion

$$\mathbf{q}^{conv} = \frac{1}{V} \sum_i m_{eff,i} c_{p,i} T_{vol,avg,i} \mathbf{v}_i$$





- **Transferred** thermal energy to the environment, fixed  $T_{enviro}$ , fixed Biot number

$$q^{trans,i} = \alpha (T_i - T_{f,i})$$

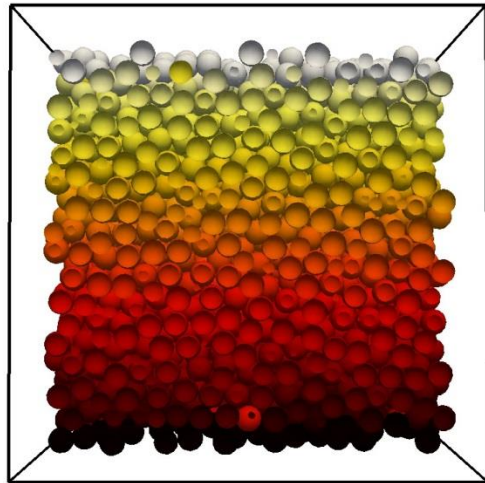
- **Particle-Particle radiative** flux currently not considered. Energy emission **does not heat particles**.

$$q_s = -\lambda_p \frac{\partial T}{\partial y}$$

- **Reference heat flux** equals flux in the pure solid



# Simulation Method



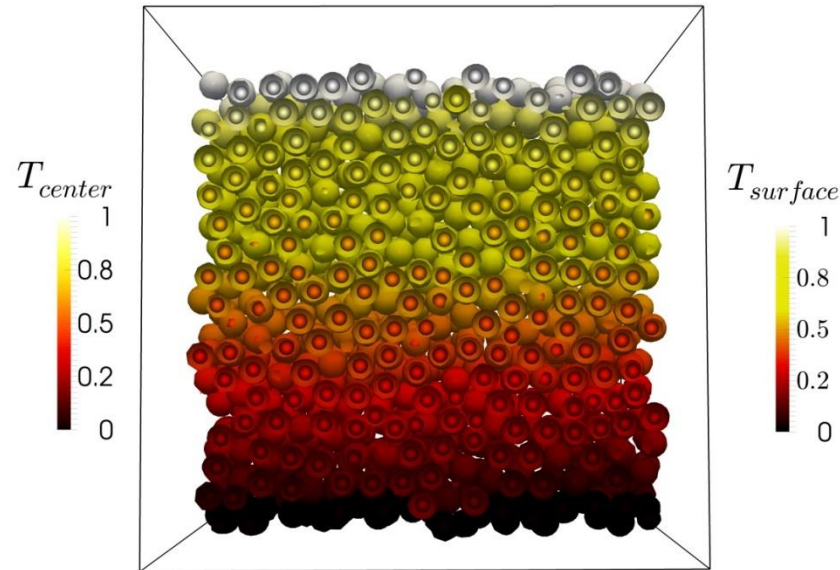
**LIGGGHTS**  
particle motion



+

**parScale**

**ParScale**  
intra-particle  
temperature  
profile

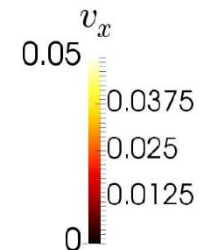
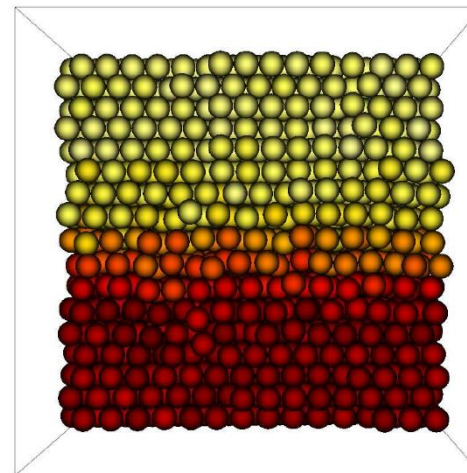
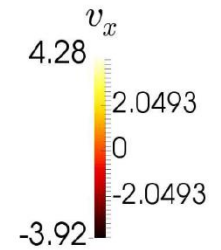
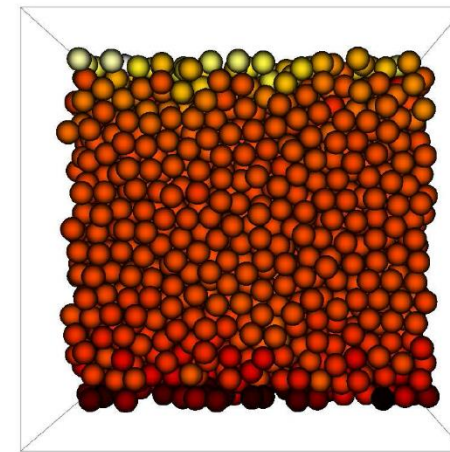
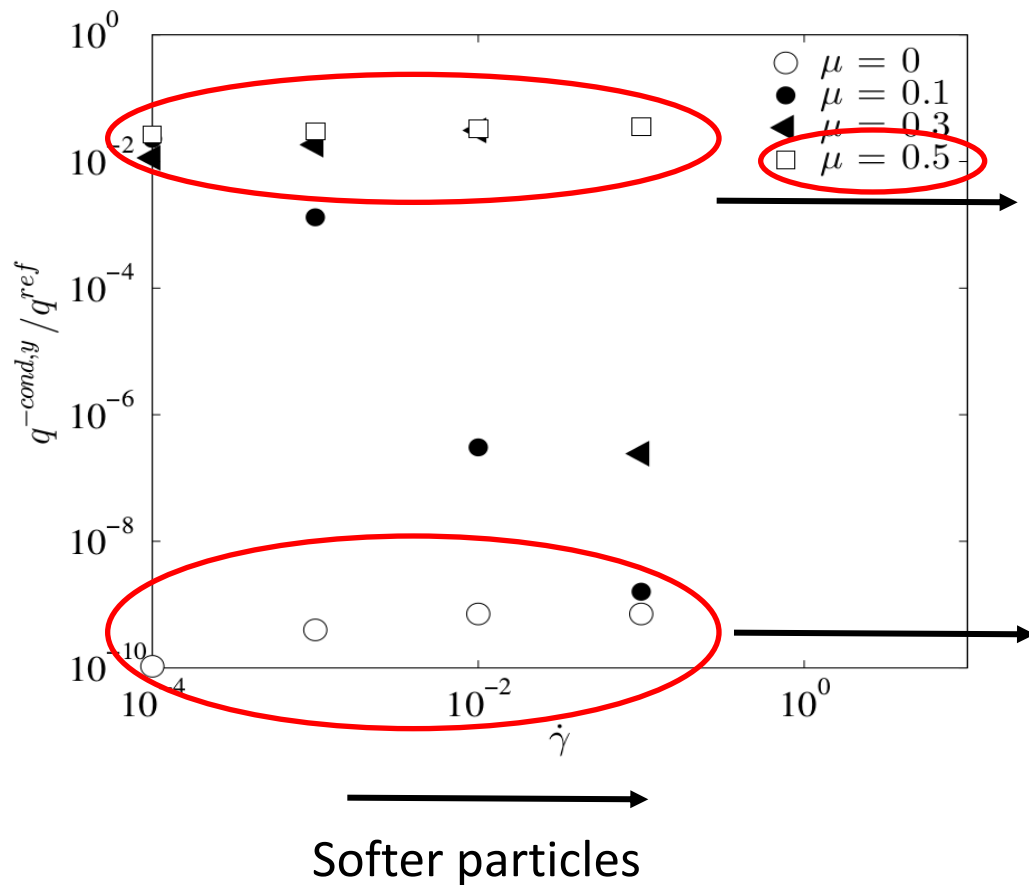


# Results

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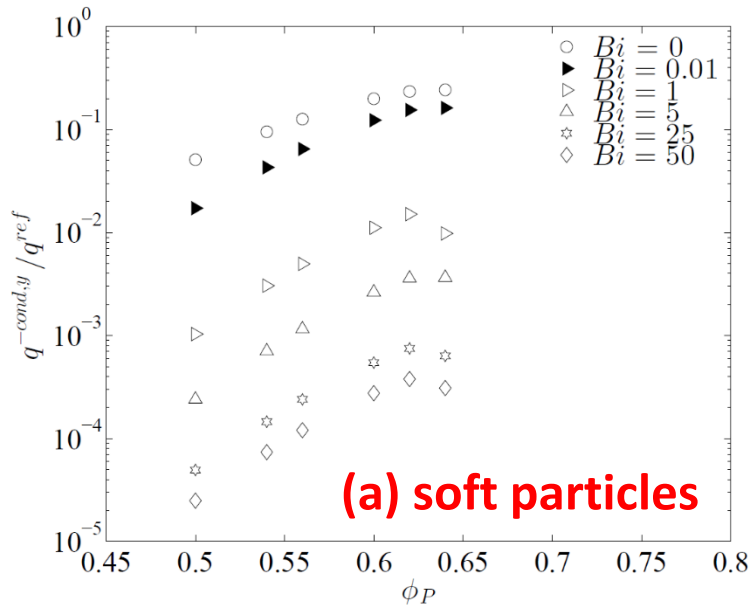
## Crystallized versus Non-crystallized Flow

$Pe = 0.01, Bi = 0.1, \phi_p = 0.64$



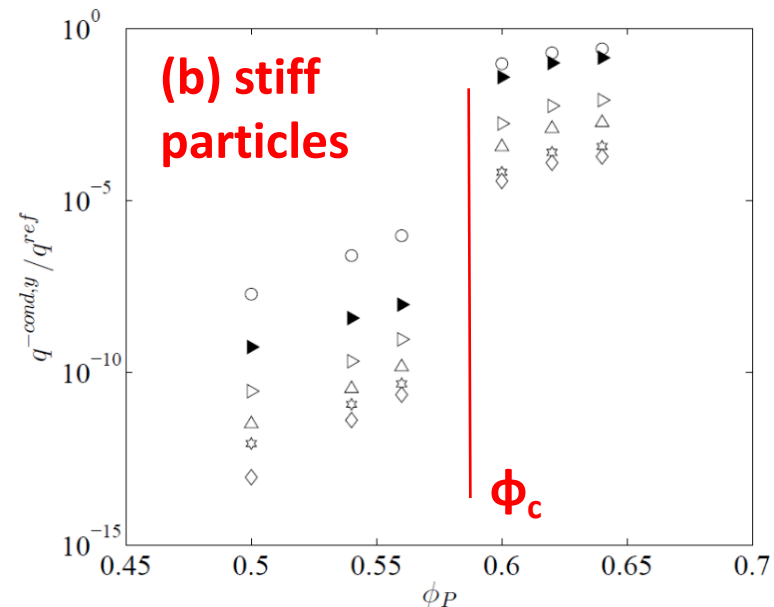
## Scaled conductive flux

$Pe = 0.01$ , (a)  $\dot{\gamma} = 10^{-1}$ , (b)  $\dot{\gamma} = 10^{-4}$



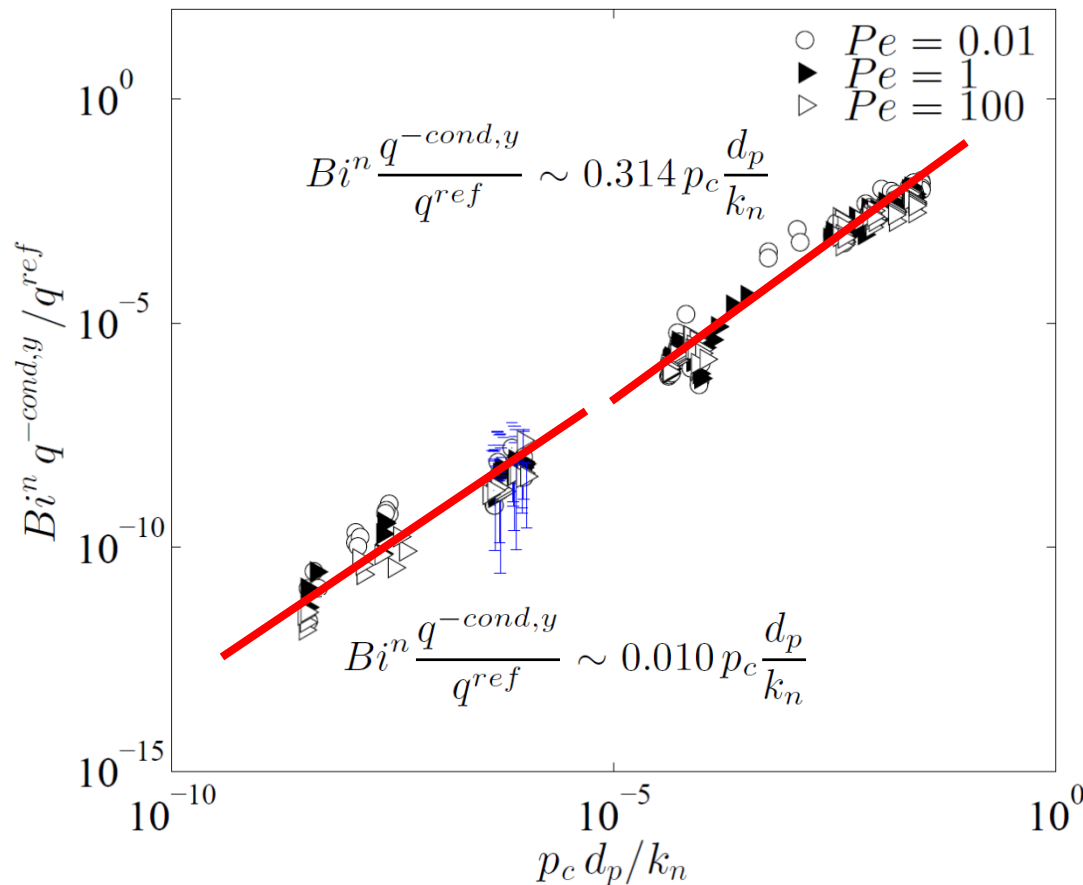
- Significant **increase of the conductive thermal transport rate** in case of jamming
- Critical jamming volume fraction depends on **particle stiffness**

- Effect seen for **all Biot numbers**
- Critical volume fraction does not depend on **Peclet** number



## Conductive flux versus Dimensionless Contact Pressure

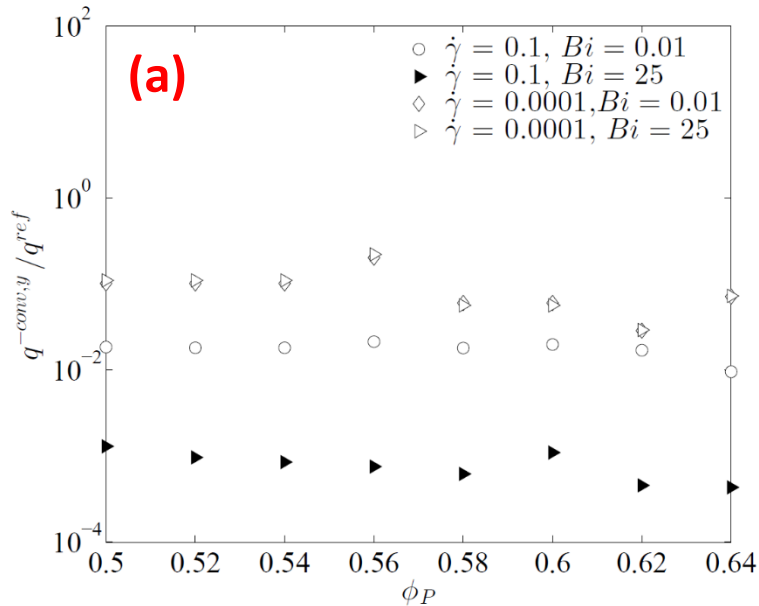
$n \sim 4/5$  leads to a collapse of all data



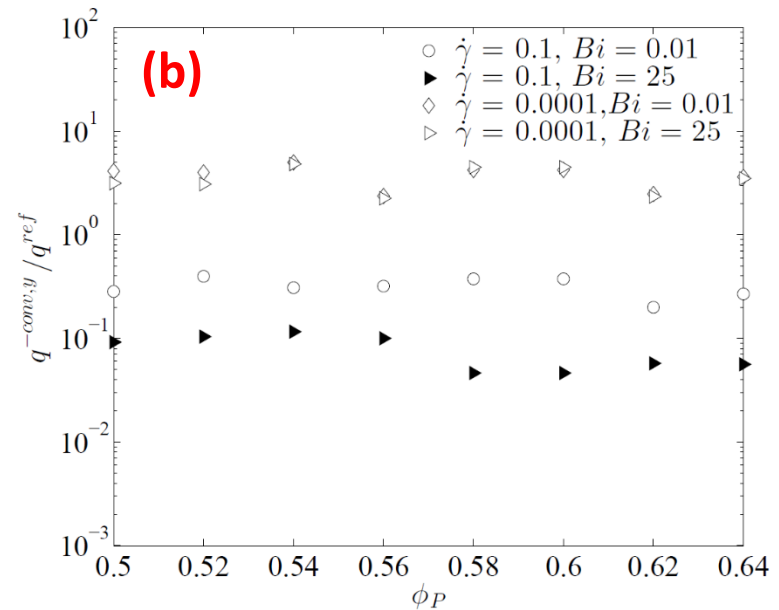
- **Correlate** dimensionless conductive flux with dimensionless contact pressure
- Increase in dimensionless contact pressure in jammed system **explains high conductive heat flux**
- **Large fluctuations** in pressure and heat flux when transitioning between regimes

## Convective flux versus Particle Concentration

(a)  $Pe = 1$ , (b)  $Pe = 100$



- **Convective flux unaffected** by change of particle concentration
- No significant effect due to jamming transition



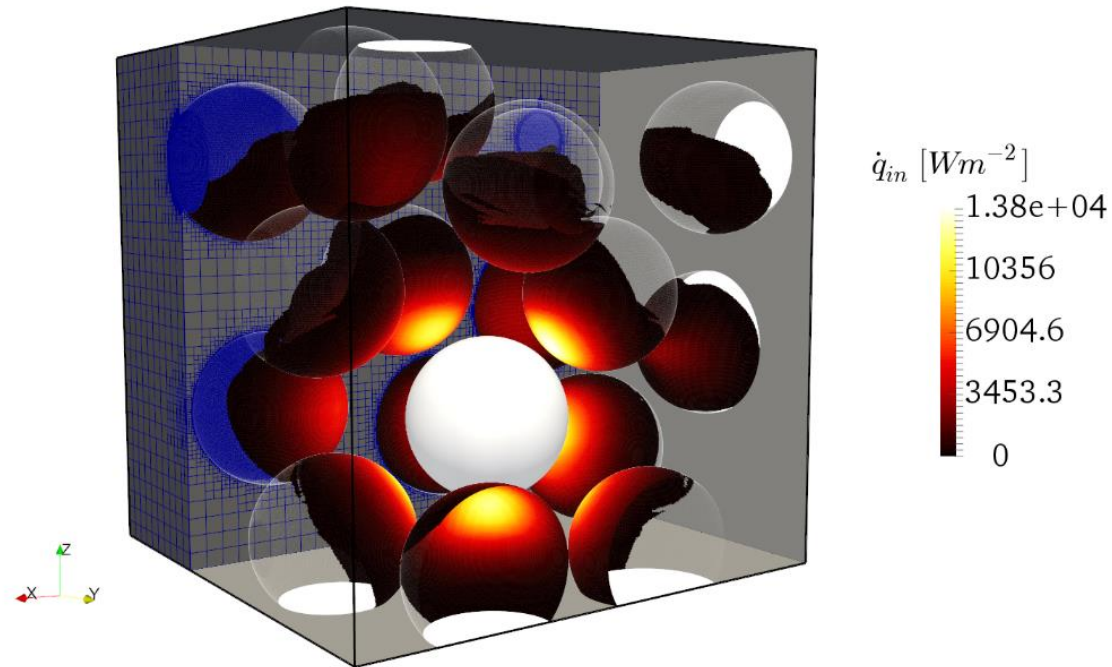
- Nearly **independent of Biot number** for stiff particles
- **Peclet number** key for modeling convective flux

# Conclusion & Outlook



# Conclusion & Outlook

- Detailed simulation of **convective, conductive, and transferred** thermal fluxes **including intra-particle temperature** profiles
- **Drastic increase of the conductive flux** in a jammed system. **Closure relationship** for conductive flux provided based on contact pressure
- **Convective** flux unaffected by jamming
- Current research focus: **include radiation** by fast algorithm to quantify shadowing effect
- More: PTF poster session, **Tue, Nov 15<sup>th</sup>, 6.00 p.m.**



# Thermal Fluxes in Wall Bounded Sheared Granular Beds Near the Jamming Point

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**Thank You!**  
**Questions?**

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