



# Malleable Cryptography for Security and Privacy in the Cloud

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# Talk Outline



- Brief overview of the PRISMALCLOUD project
- Challenges in dynamic cloud environments
- Malleable cryptographic primitives
  - Encryption and signatures
- Applications within PRISMACLOUD
  - Homomorphic proxy re-cryptography
  - Multikey-homomorphic cryptography

# PRISMACLOUD Overview



- Improve the security and privacy of cloud based services and make them usable for providers and users
- Enable **end-to-end security** for cloud users and protect their privacy by means cryptography
- Bring novel cryptographic concepts and methods to practical application
- The project is a huge undertaking and produces outcome in many different disciplines and layers
- Today, the focus is on a particular aspect of the project

# Project Metadata



Call: H2020-ICT-2014-1

Acronym: PRISMACLOUD

Type of Action: RIA

Number: 644962

Partners: 16

Duration: 42 months

Start Date: 2015-02-01

Estimated Project Cost: approx. 8.5M Euro

Requested EU Contribution: approx. 8M Euro

Coordinator: Austrian Institute of Technology GmbH



# PRISMACLOUD Partners



leti

etra I+D



Atos

The PRISMACLOUD consortium is composed of a balanced team of  
**6 industrial partners,**  
**2 industrial research centres,**  
**2 institutional research organisations and**  
**6 universities.**

interoute  
from the ground to the cloud

IAIK

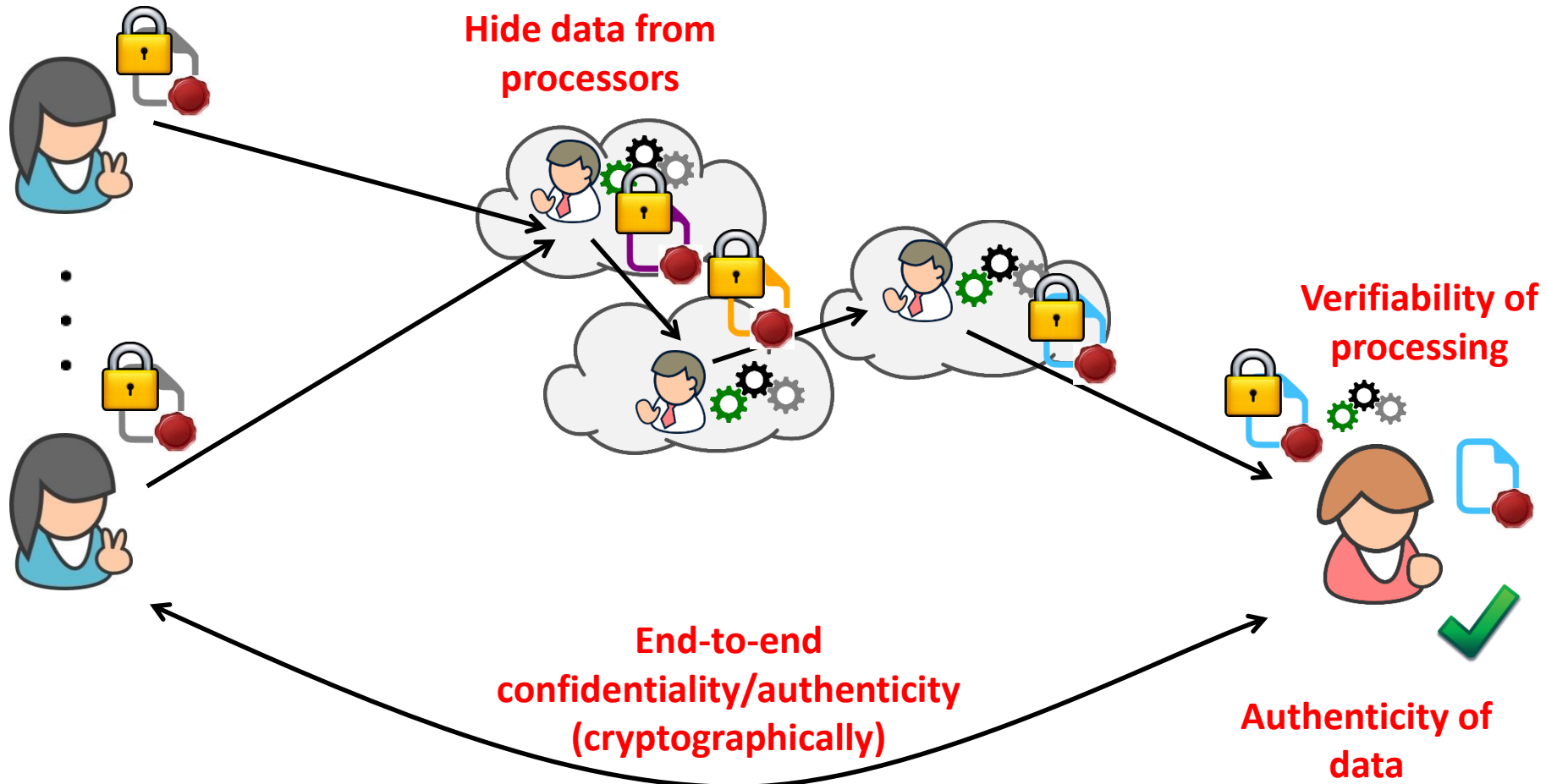


TECHNISCHE  
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DARMSTADT

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SECURE TECHNOLOGIES



# Dynamic Cloud Environment: Composition of Services



# How to Realize Such Features?



- What is the issue when end-to-end guarantees are required?
  - Never decrypt in transit
  - Never lose the data origin protection (authenticity) in transit
- Need adequate cryptographic primitives that support
  - agility
  - functionality

# Malleable Cryptography



- Let us take a cryptographic primitive, e.g., an encryption or signature scheme
- Informally, a primitive is malleable if we can manipulate its cryptographic objects (ciphertexts, signatures) in a meaningful (controlled) way without knowing the secret
  - Changing the encrypted/signed messages in a controlled way **without** the key
  - Changing the key corresponding to a ciphertext/signature
  - Combining ciphertexts/signatures under **different** keys
- Subsequently, many details are omitted for the sake of presentation



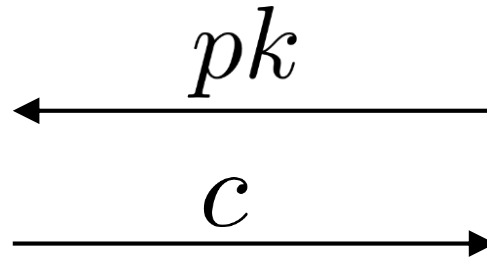
# Public Key Encryption



Alice

Bob

$$(sk, pk) \leftarrow \mathcal{G}(1^\kappa)$$



$$c \leftarrow \mathcal{E}_{pk}(m)$$

$$m \leftarrow \mathcal{D}_{sk}(c)$$

# Homomorphic Encryption



- Operations performed on ciphertexts “carry over” to the underlying plaintexts
- Allows to evaluate a class of functions on ciphertexts
- Scheme  $(\mathcal{G}, \mathcal{E}, \mathcal{D})$  comes with an additional evaluation algorithm  $\mathcal{EV}$  such that for all functions  $f \in \mathcal{F}$

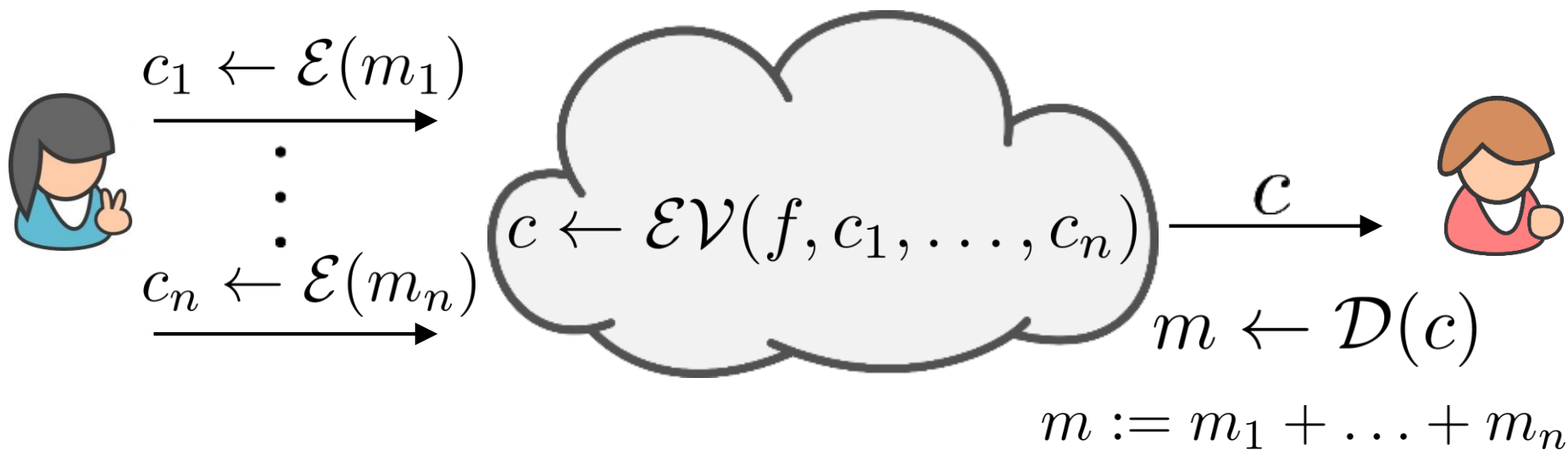
$$f(m_1, \dots, m_n) = \mathcal{D}(\mathcal{EV}(f, \mathcal{E}(m_1), \dots, \mathcal{E}(m_n)))$$

- If  $\mathcal{F}$  covers all computable functions: FHE

# Simple Example (linear Functions)



- Adding up encrypted values, e.g., measurements
- Function  $f$  represents the sum



# Multikey-Homomorphic Encryption



- Homomorphic encryption scheme that can evaluate functions on ciphertexts under **different** public keys
- Decryption requires **all** respective private keys

$$f(m_1, \dots, m_n) = \mathcal{D}_{sk_1, \dots, sk_n}(\mathcal{EV}(f, \mathcal{E}_{pk_1}(m_1), \dots, \mathcal{E}_{pk_n}(m_n)))$$

- We investigate a related concept based on homomorphic proxy re-encryption

# Proxy Re-Encryption



- An encryption scheme  $(\mathcal{G}, \mathcal{E}, \mathcal{D})$  with additional algorithms
  - re-key generation  $rk_{A \rightarrow B} \leftarrow \mathcal{RG}(sk_A, pk_B)$
  - re-encryption  $c_B \leftarrow \mathcal{RE}(rk_{A \rightarrow B}, c_A)$

$$(sk_A, pk_A) \leftarrow \mathcal{G}(1^\kappa)$$

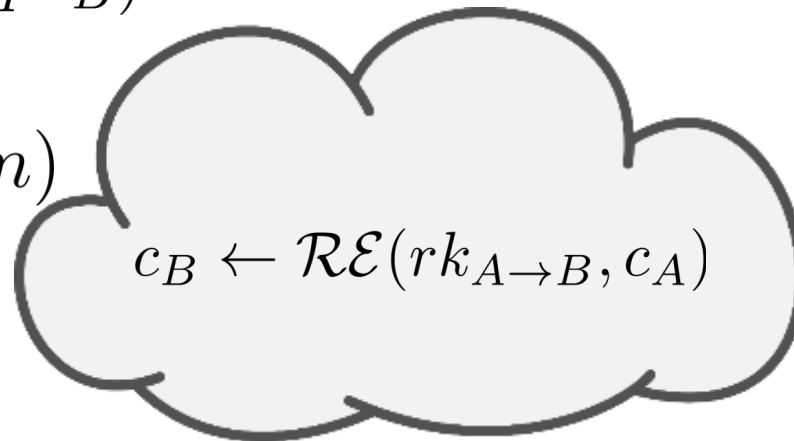
$$rk_{A \rightarrow B} \leftarrow \mathcal{RG}(sk_A, pk_B)$$

$$(sk_B, pk_B) \leftarrow \mathcal{G}(1^\kappa)$$

$$rk_{A \rightarrow B}$$



$$c_A \leftarrow \mathcal{E}_{pk_A}(m)$$



$$c_B$$



$$m \leftarrow \mathcal{D}_{sk_B}(c_B)$$

# Homomorphic Proxy Re-Encryption



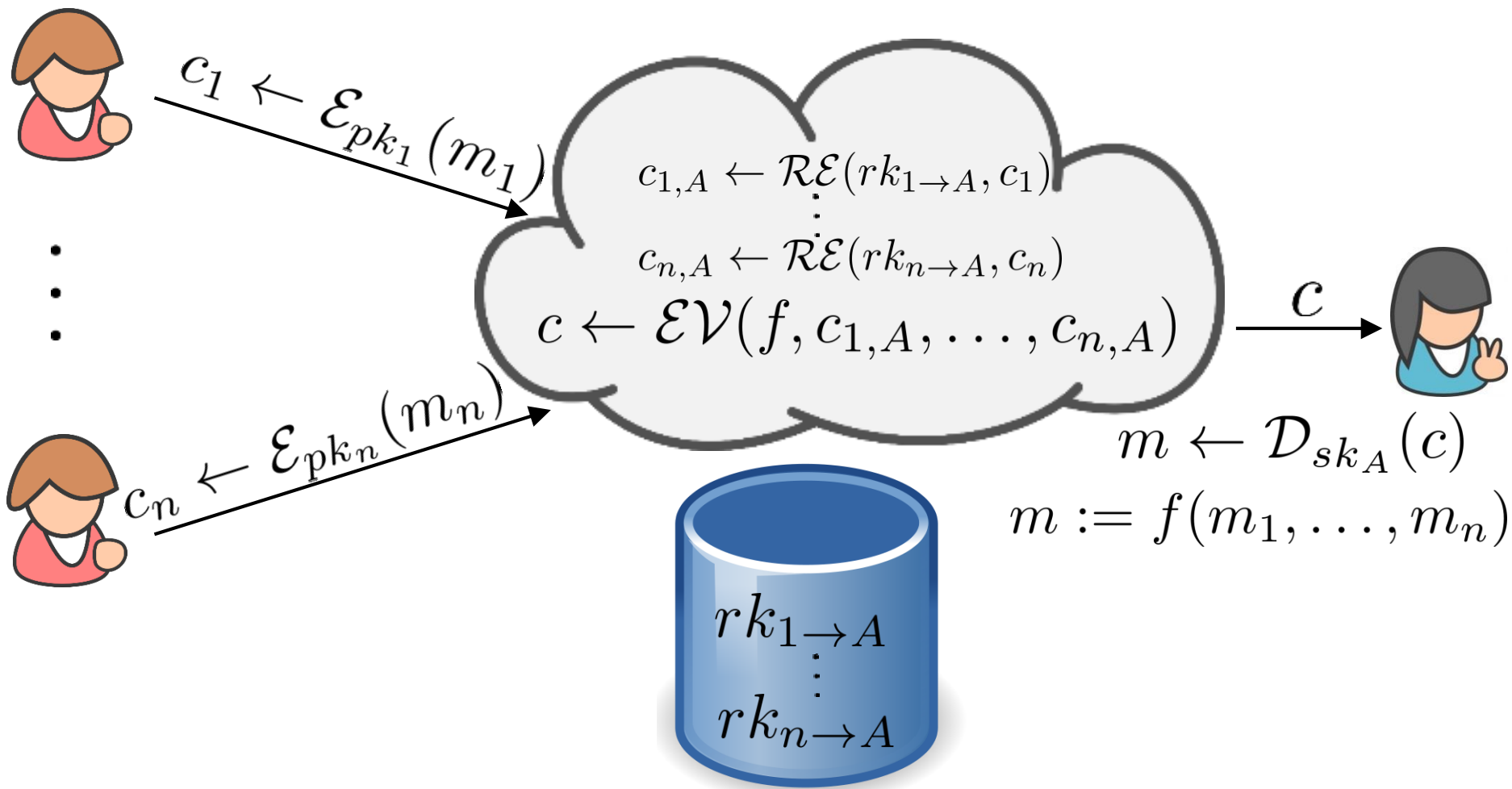
- A PRE scheme  $(\mathcal{G}, \mathcal{E}, \mathcal{D}, \mathcal{RE}, \mathcal{RE})$  that is homomorphic with respect to a class of functions
- Scheme comes with evaluation algorithm  $\mathcal{EV}$

$$f(m_1, \dots, m_n) = \mathcal{D}(sk_A, \mathcal{EV}(f, \mathcal{E}_{pk_A}(m_1), \dots, \mathcal{E}_{pk_A}(m_n)))$$

- Under the correctness of the PRE, if re-keys  $rk_{i \rightarrow A}$  for ciphertexts  $c_i \leftarrow \mathcal{E}_{pk_i}(m_i)$  are available

$$f(m_1, \dots, m_n) = \mathcal{D}(sk_A, \mathcal{EV}(f, \mathcal{RE}(rk_{1 \rightarrow A}, c_1), \dots, \mathcal{RE}(rk_{n \rightarrow A}, c_n)))$$

# Homomorphic PRE Example



# What do we achieve so far?



- Only confidentiality guarantees, but no means to preserve verifiability of operations/computations on data in transit
- Neither do we get authenticity guarantees
- Now we consider the same “stack” for signatures (authenticators)
- And then briefly discuss how to combine them and what this will give us



# Digital Signatures



Alice



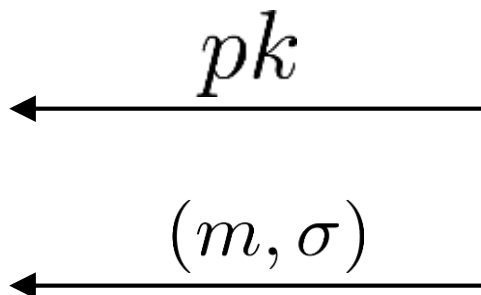
$$\mathcal{V}_{pk}(m, \sigma) \in \{0, 1\}$$

Bob

$$(sk, pk) \leftarrow \mathcal{G}(1^\kappa)$$



$$\sigma \leftarrow \mathcal{S}_{sk}(m)$$



- In a message authentication code (MAC) there is a secret key shared by Alice and Bob and verification also requires the secret key

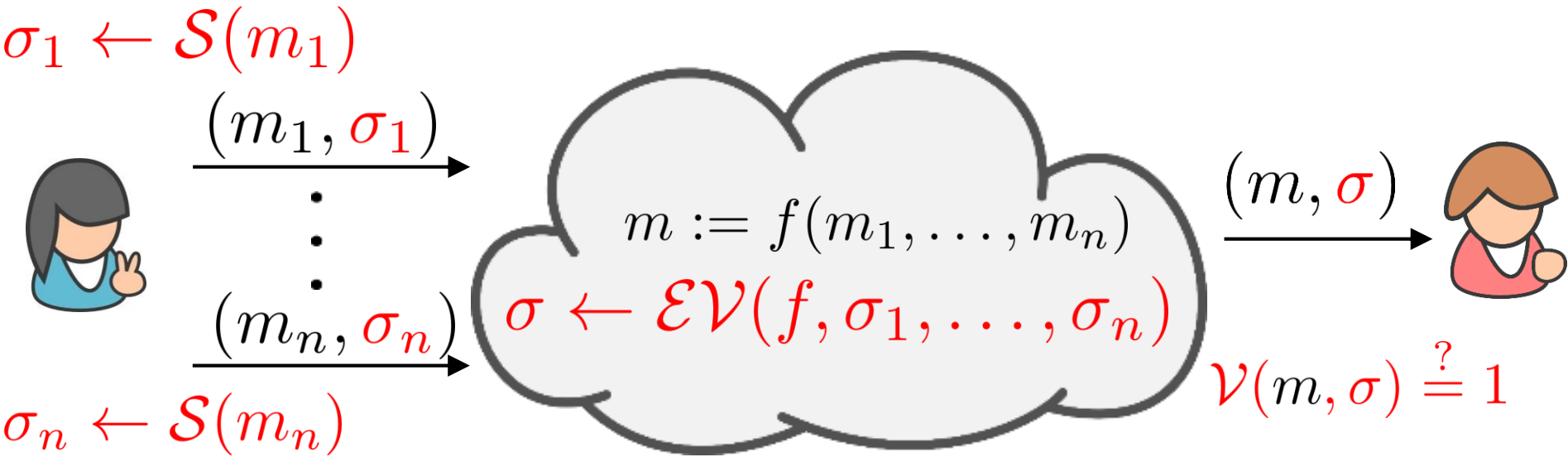
# Homomorphic Signatures



- Operations performed on signatures “carry over” to the signed messages
- Allows to evaluate a class of functions on signatures
- Scheme  $(\mathcal{G}, \mathcal{S}, \mathcal{V})$  comes with an additional evaluation algorithm  $\mathcal{EV}$  such that for all functions  $f \in \mathcal{F}$

$$\mathcal{V}(f(m_1, \dots, m_n), \mathcal{EV}(f, \mathcal{S}(m_1), \dots, \mathcal{S}(m_n))) = 1$$

# Homomorphic Signatures Example



# Multikey-Homomorphic Signatures



- Homomorphic signature scheme that can evaluate functions on signatures under **different** public keys
- Verification requires **all** respective public keys (or a compact representation of a key set) denoted **pk**

$$\mathcal{V}_{\mathbf{pk}}(f(m_1, \dots, m_n), \mathcal{EV}(f, \mathcal{S}_{pk_1}(m_1), \dots, \mathcal{S}_{pk_n}(m_n))) = 1$$

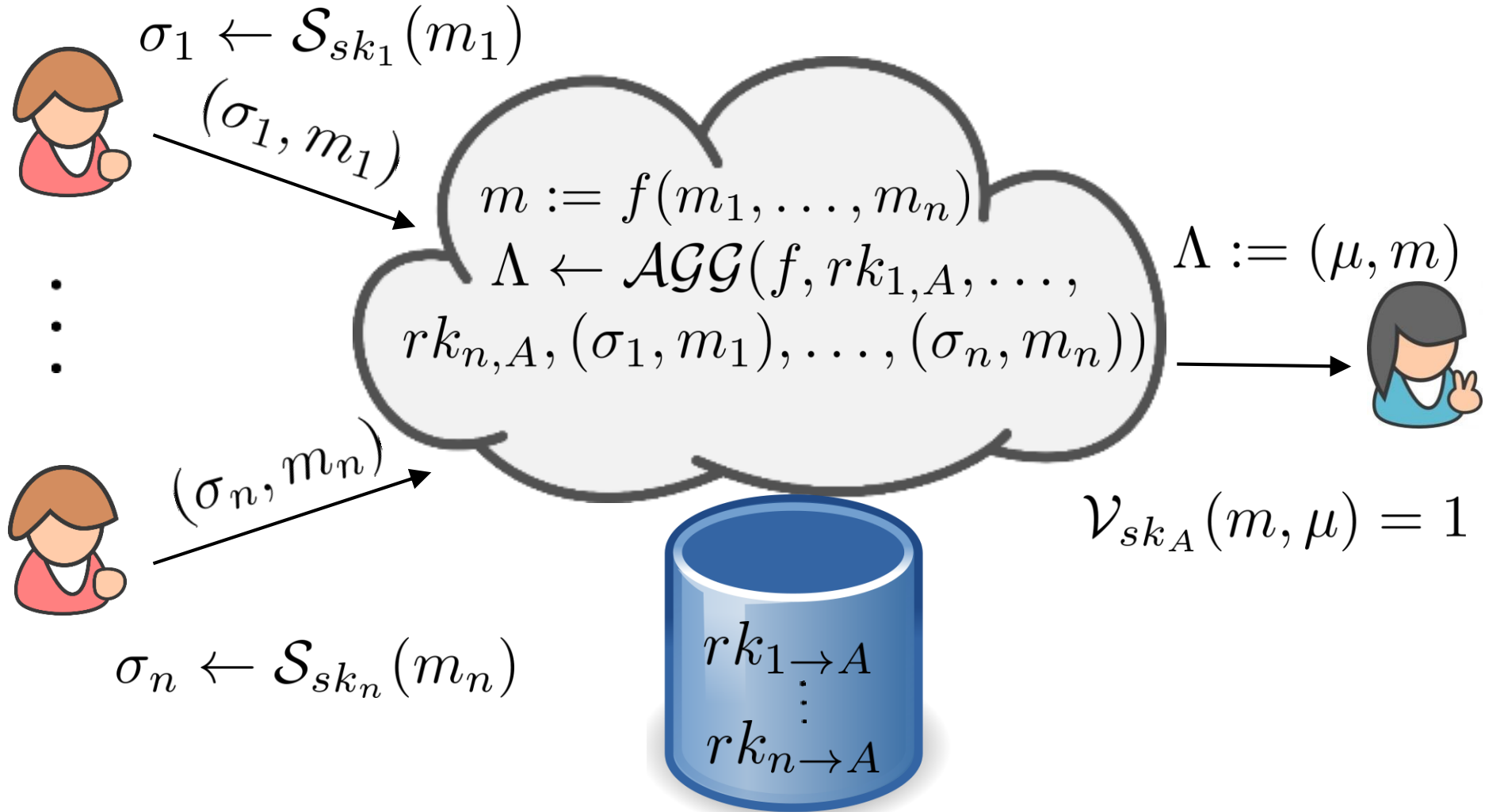
- We investigate a related concept based on homomorphic proxy re-authenticators

# Proxy Re-Authenticators



- A combination of a signature scheme and a message authentication code (MAC)
- “Signature to MAC keys” given to a proxy
- Proxy can perform re-operations from signatures to MACs
- The final result is privately verifiable
- There are also proxy re-signatures
  - No approach/construction is compatible with homomorphic properties

# Homomorphic Proxy Re-Authenticators



# Combining Both Tools



- Homomorphic PRAs do neither hide inputs nor outputs from proxy
- So far no multikey-homomorphic concept that combines encryption and authentication
- We can combine homomorphic PRAs with homomorphic PREs
  - Obtain a general framework of homomorphic proxy re-cryptography
- Prior work
  - Verifiable homomorphic encryption [LDPW14] (only under a single key)
  - Private and unforgeable data aggregation [LEÖM15] (only sum of inputs; common setup – shared key)

# Input and Output Privacy of Homomorphic PRAs



- We must not send  $(\sigma_1, m_1)$  directly
  - Using homomorphic PRE for messages not sufficient
  - Signatures may still leak messages
- Need some technical tricks
  - Use homomorphic PRE to encrypt extended message (additional random message)
  - Use PRA to sign extended message and do not leak randomness
  - Constructions not fully black-box



# Conclusions



- Homomorphic proxy re-cryptography
  - Homomorphic proxy re-encryption
  - Homomorphic proxy re-authenticators
- Allows us to support confidentiality and verifiability in a multi-key (-source) setting
- In contrast to multikey-homomorphic primitives, we have a single independent key for decryption/verification
- Many interesting open questions

# References



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